

Machine-Learning-Guided Adaptive Program Analysis

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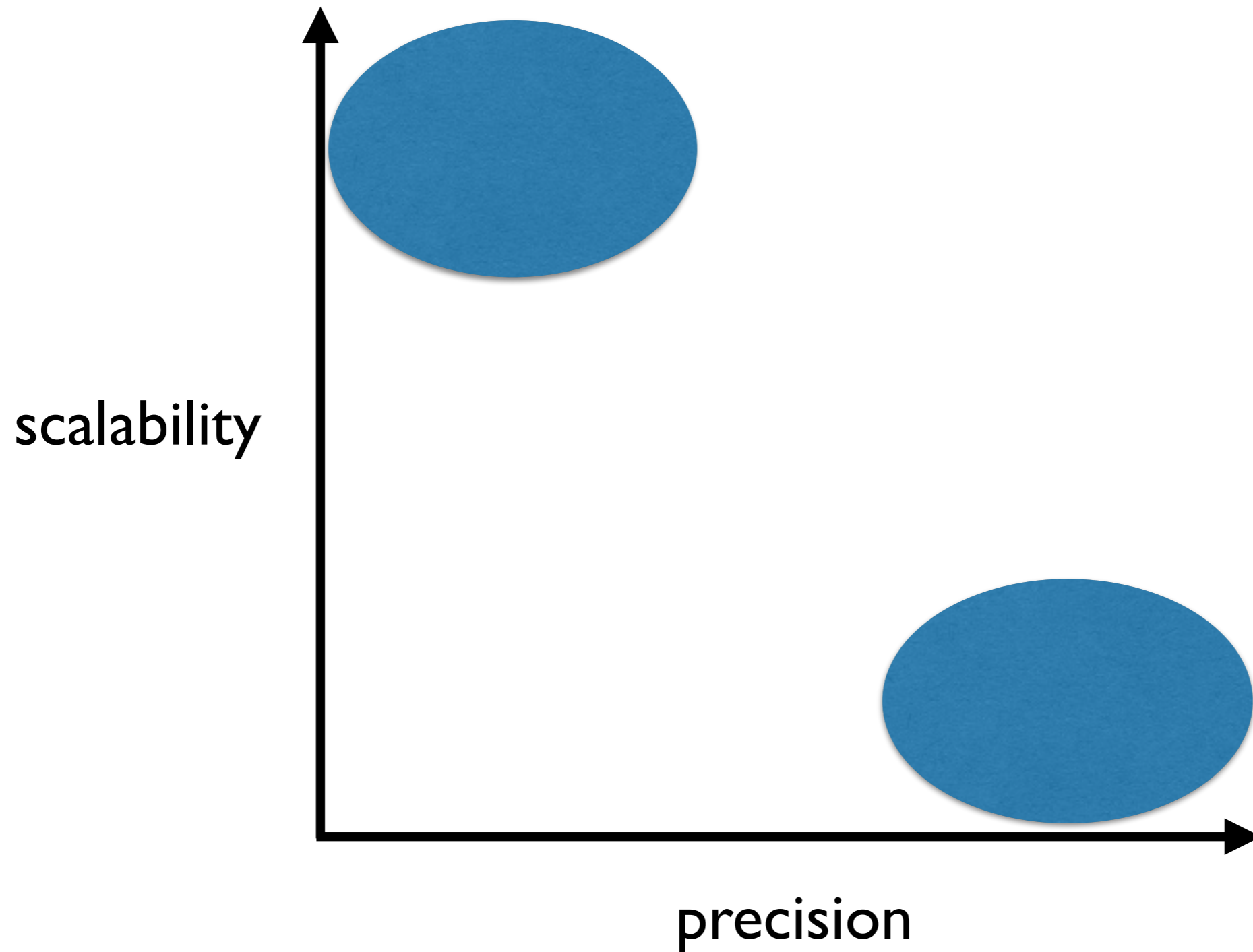
Hongseok Yang

Oxford University

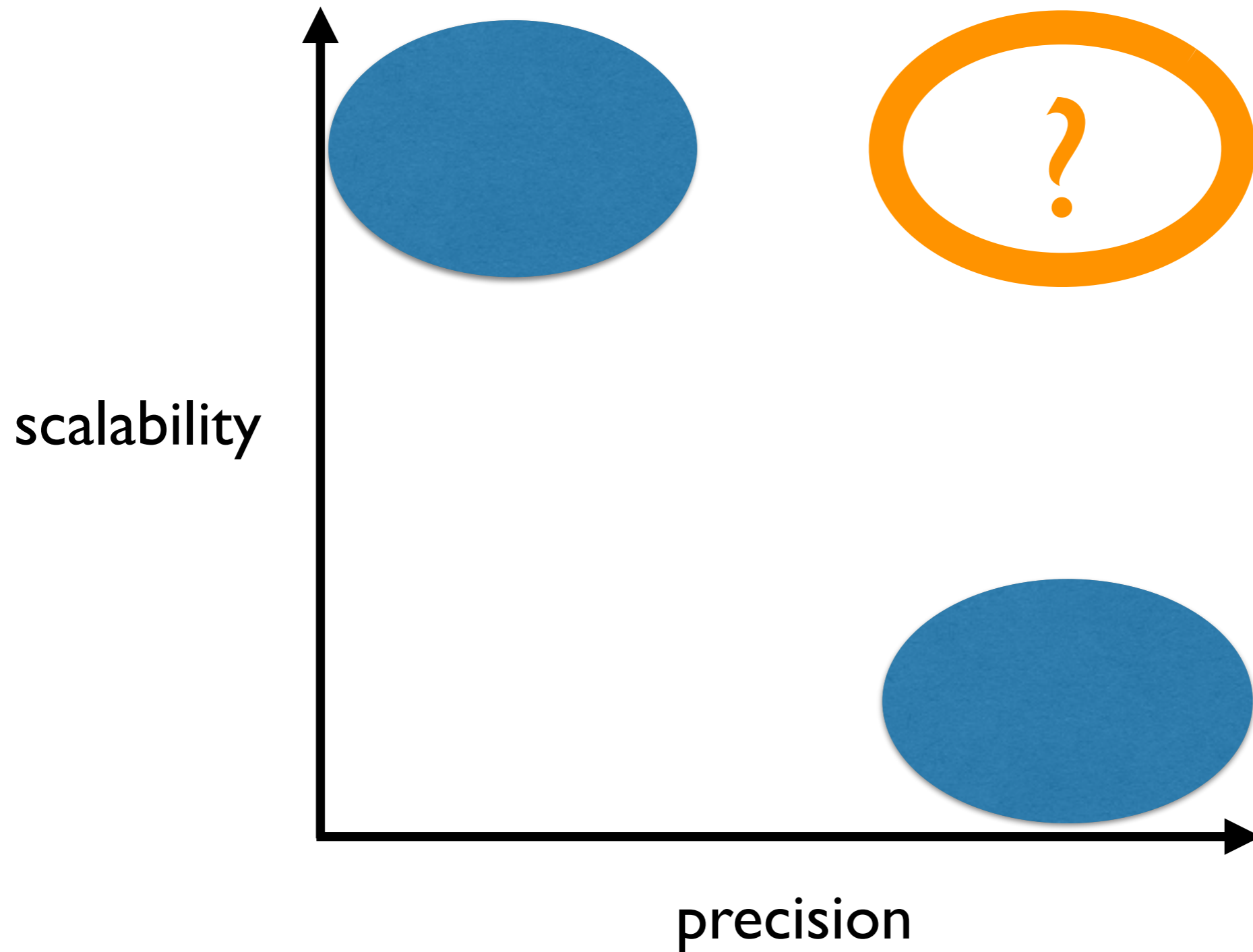


7 September 2016
TAPAS 2016 @ Edinburgh, Scotland

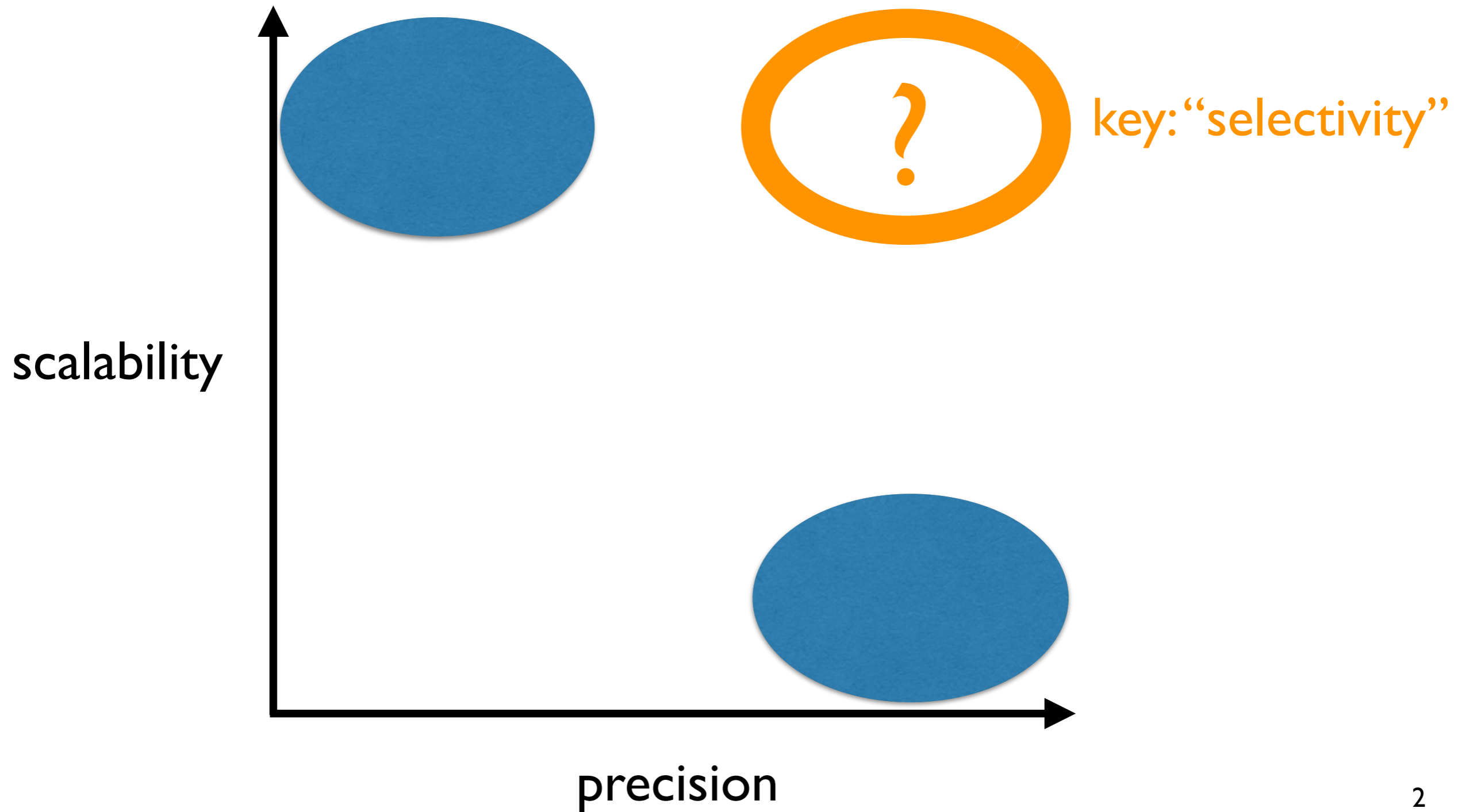
Challenge in Static Analysis



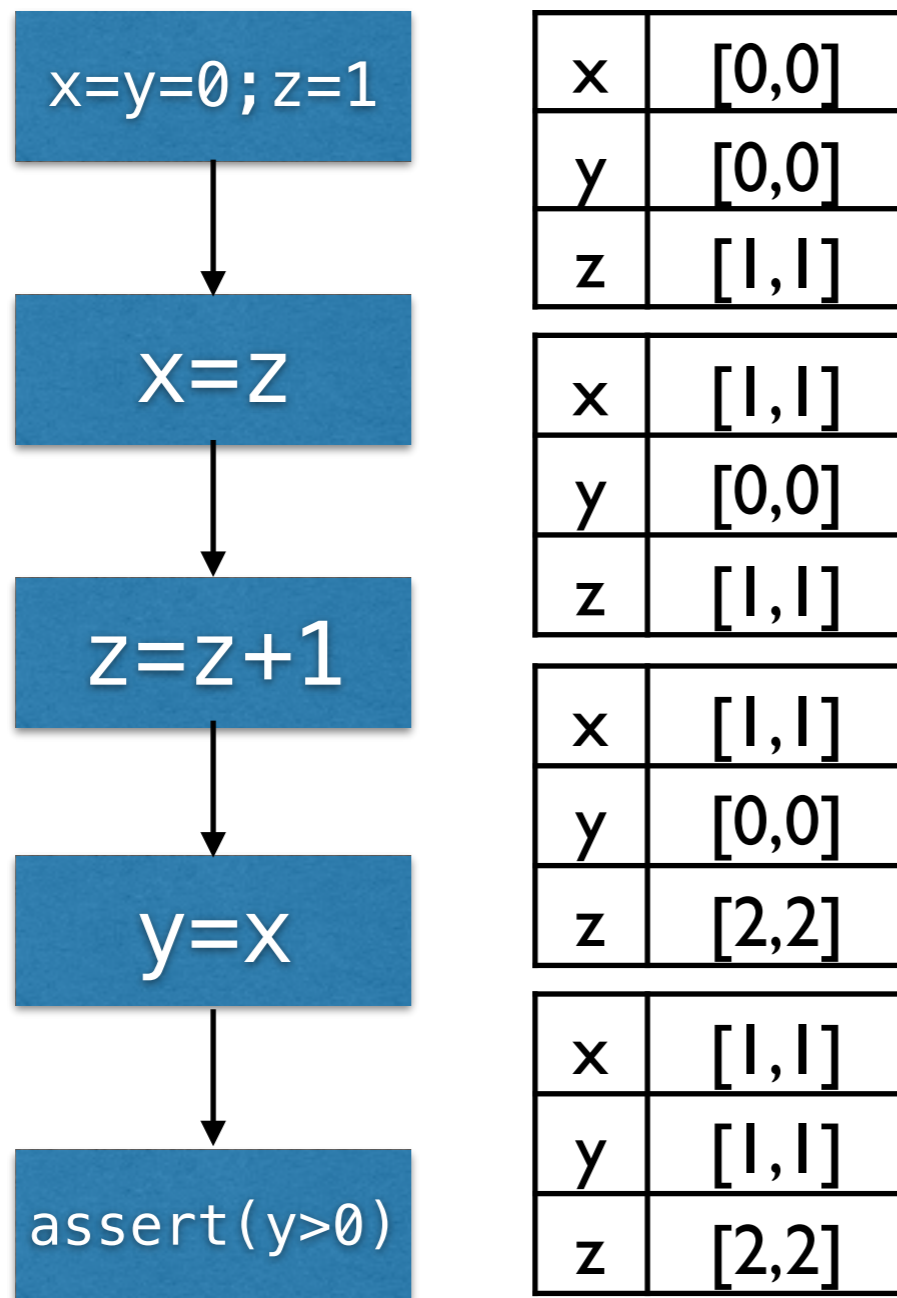
Challenge in Static Analysis



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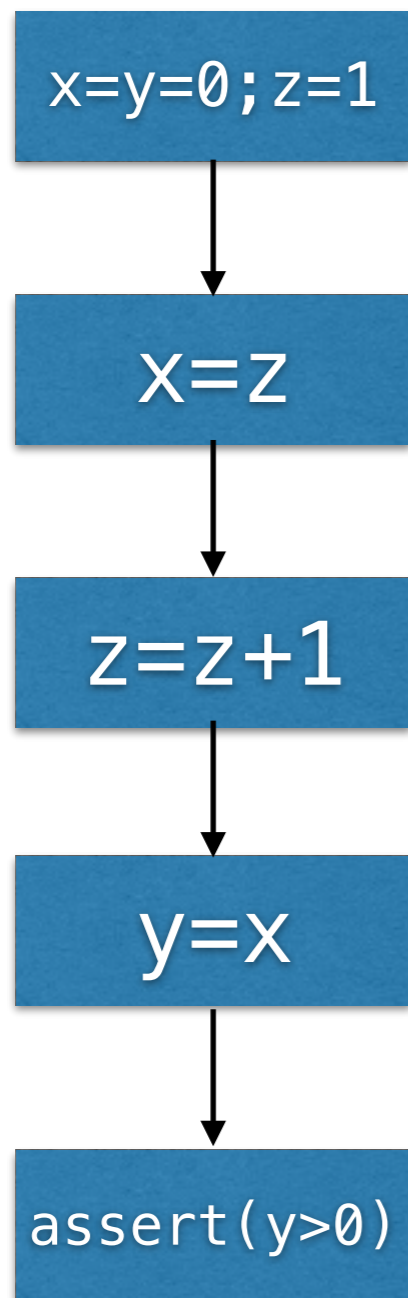


Flow-Sensitivity



precise but costly

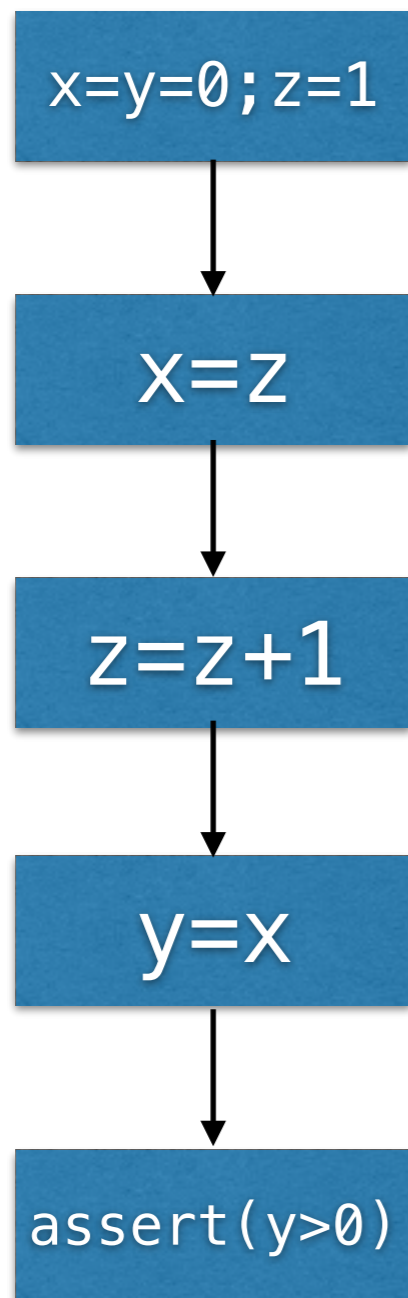
Flow-Insensitivity



| | |
|---|----------------|
| x | $[0, +\infty]$ |
| y | $[0, +\infty]$ |
| z | $[1, +\infty]$ |

cheap but imprecise

Selective Flow-Sensitivity



FS : {x,y}

| | |
|---|-------|
| x | [0,0] |
| y | [0,0] |

| | |
|---|--------|
| x | [1,+∞] |
| y | [0,0] |

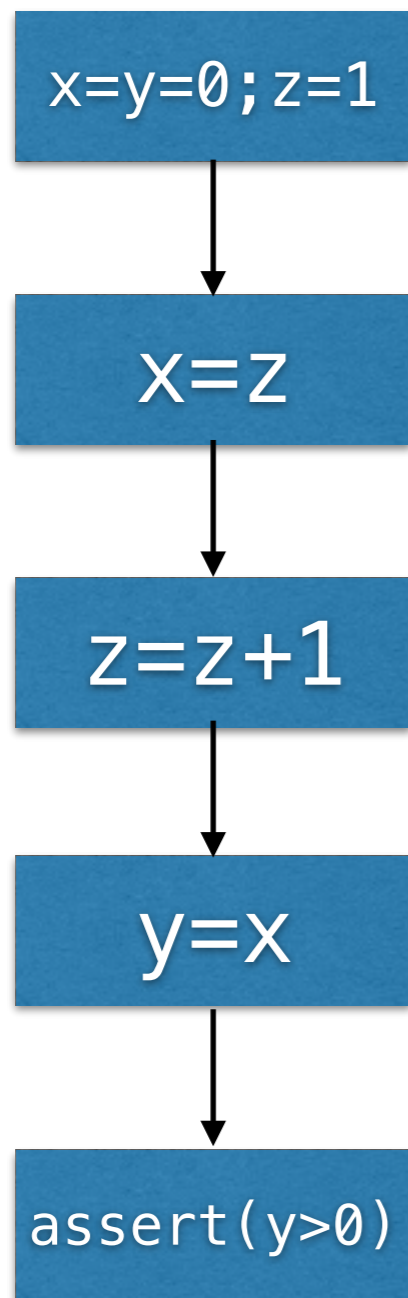
| | |
|---|--------|
| x | [1,+∞] |
| y | [0,0] |

| | |
|---|--------|
| x | [1,+∞] |
| y | [1,+∞] |

FI : {z}

| | |
|---|--------|
| z | [1,+∞] |
|---|--------|

Selective Flow-Sensitivity



FS : {y,z}

| | |
|---|-------|
| y | [0,0] |
| z | [1,1] |

| | |
|---|-------|
| y | [0,0] |
| z | [1,1] |

| | |
|---|-------|
| y | [0,0] |
| z | [2,2] |

| | |
|---|--------|
| y | [0,+∞] |
| z | [2,2] |

FI : {x}

| | |
|---|--------|
| x | [0,+∞] |
|---|--------|

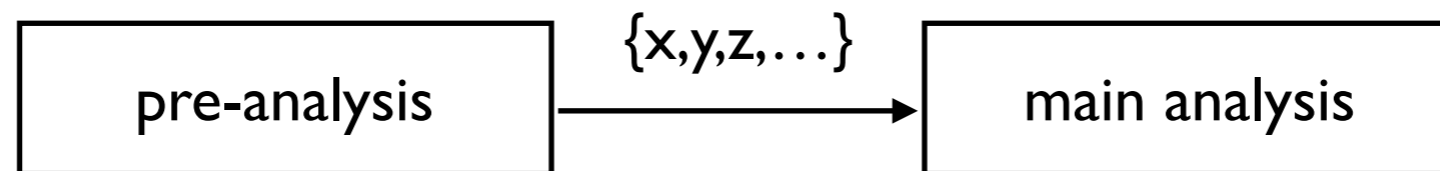
fail to prove

Hard Search Problem

- Intractably large space, if not infinite
 - 2^{Var} different abstractions for FS
- Most of them are too imprecise or costly
 - $P(\{x,y,z\}) = \{\emptyset, \cancel{\{x\}}, \cancel{\{y\}}, \cancel{\{z\}}, \{x,y\}, \{y,z\}, \{x,z\}, \{x,y,z\}\}$

Our Research

- How to automatically find a good abstraction?
 - pre-analysis [PLDI'14, TOPLAS'16]



- machine learning techniques [OOPSLA'15, SAS'16, APLAS'16]



Our Learning Approaches

- Learning via black-box optimization [OOPSLA'15]
- Learning via white-box optimization [APLAS'16]
- Learning from automatically labelled data [SAS'16]
- Learning with automatically generated features (in progress)
- ...

Static Analyzer

$$F(p, a) \Rightarrow n$$

abstraction
(e.g., a set of variables)

number of
proved assertions

OOPSLA'15

Our Learning Approach

Our Learning Approach

- Parameterized adaptation strategy

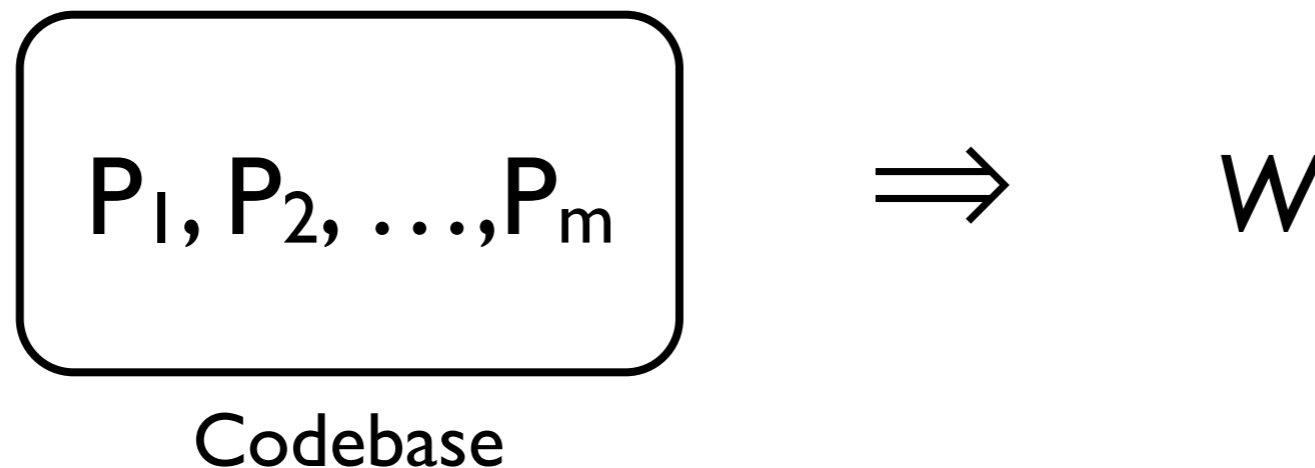
$$S_w : \text{pgm} \rightarrow 2^{\text{Var}}$$

Our Learning Approach

- Parameterized adaptation strategy

$$S_w : \text{pgm} \rightarrow 2^{\text{Var}}$$

- Learn a good parameter W from existing codebase

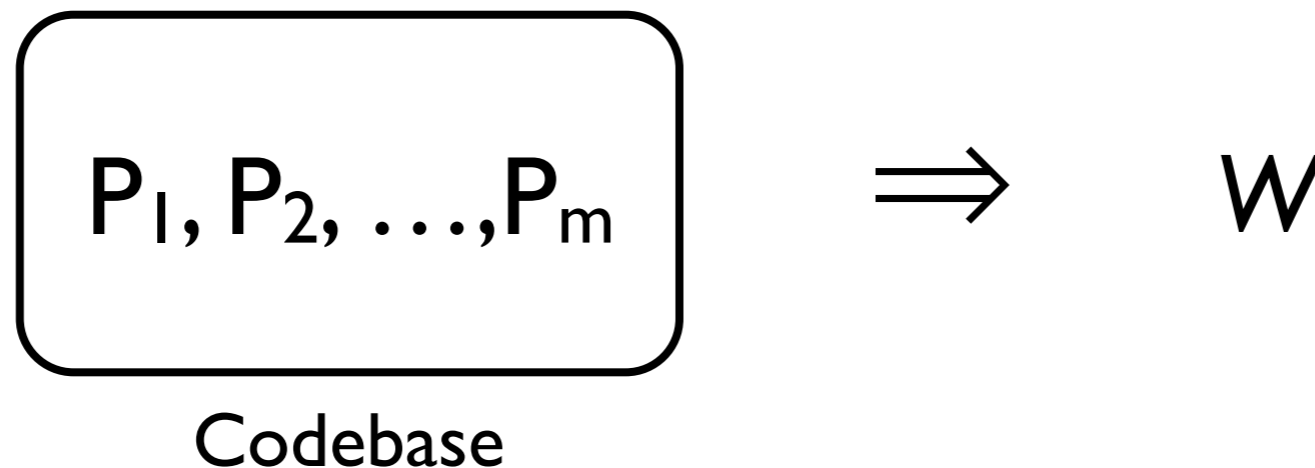


Our Learning Approach

- Parameterized adaptation strategy

$$S_w : \text{pgm} \rightarrow 2^{\text{Var}}$$

- Learn a good parameter W from existing codebase



- For new program P , run static analysis with $S_w(P)$

I. Parameterized Strategy

$$S_w : \text{pgm} \rightarrow 2^{\text{Var}}$$

- (1) Represent program variables as feature vectors.
- (2) Compute the score of each variable.
- (3) Choose the top-k variables based on the score.

(I) Features

- Predicates over variables:

$$f = \{f_1, f_2, \dots, f_5\} \quad (f_i : \text{Var} \rightarrow \{0, 1\})$$

- 45 simple syntactic features for variables: e.g,
- local / global variable, passed to / returned from malloc, incremented by constants, etc

(I) Features

- Represent each variable as a feature vector:

$$f(\mathbf{x}) = \langle f_1(\mathbf{x}), f_2(\mathbf{x}), f_3(\mathbf{x}), f_4(\mathbf{x}), f_5(\mathbf{x}) \rangle$$

$$f(\mathbf{x}) = \langle 1, 0, 1, 0, 0 \rangle$$

$$f(\mathbf{y}) = \langle 1, 0, 1, 0, 1 \rangle$$

$$f(\mathbf{z}) = \langle 0, 0, 1, 1, 0 \rangle$$

(2) Scoring

- The parameter w is a real-valued vector: e.g.,

$$w = \langle 0.9, 0.5, -0.6, 0.7, 0.3 \rangle$$

- Compute scores of variables:

$$\text{score}(x) = \langle 1, 0, 1, 0, 0 \rangle \cdot \langle 0.9, 0.5, -0.6, 0.7, 0.3 \rangle = 0.3$$

$$\text{score}(y) = \langle 1, 0, 1, 0, 1 \rangle \cdot \langle 0.9, 0.5, -0.6, 0.7, 0.3 \rangle = 0.6$$

$$\text{score}(z) = \langle 0, 0, 1, 1, 0 \rangle \cdot \langle 0.9, 0.5, -0.6, 0.7, 0.3 \rangle = 0.1$$

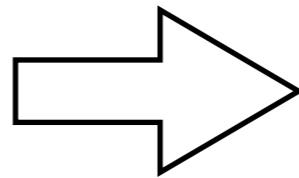
(3) Choose Top-k Variables

- Choose the top-k variables based on their scores:
e.g., when $k=2$,

$$\text{score}(x) = 0.3$$

$$\text{score}(y) = 0.6$$

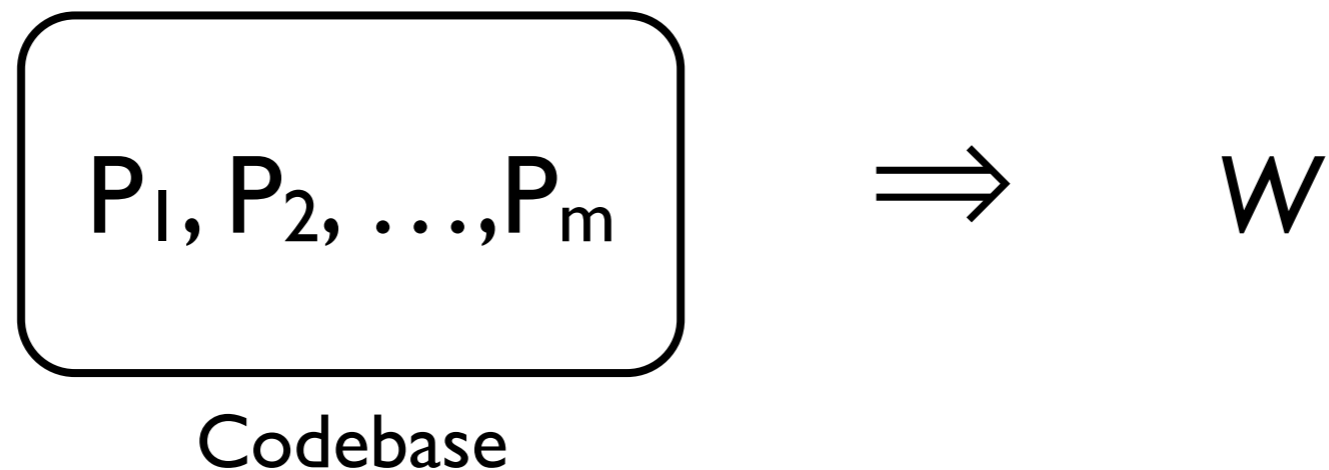
$$\text{score}(z) = 0.1$$



$\{x, y\}$

- In experiments, we chosen 10% of variables with highest scores.

2. Learn a Good Parameter



- Solve the optimization problem:

Find w that maximizes $\sum_{P_i} F(P_i, S_w(P_i))$

Learning via Random Sampling

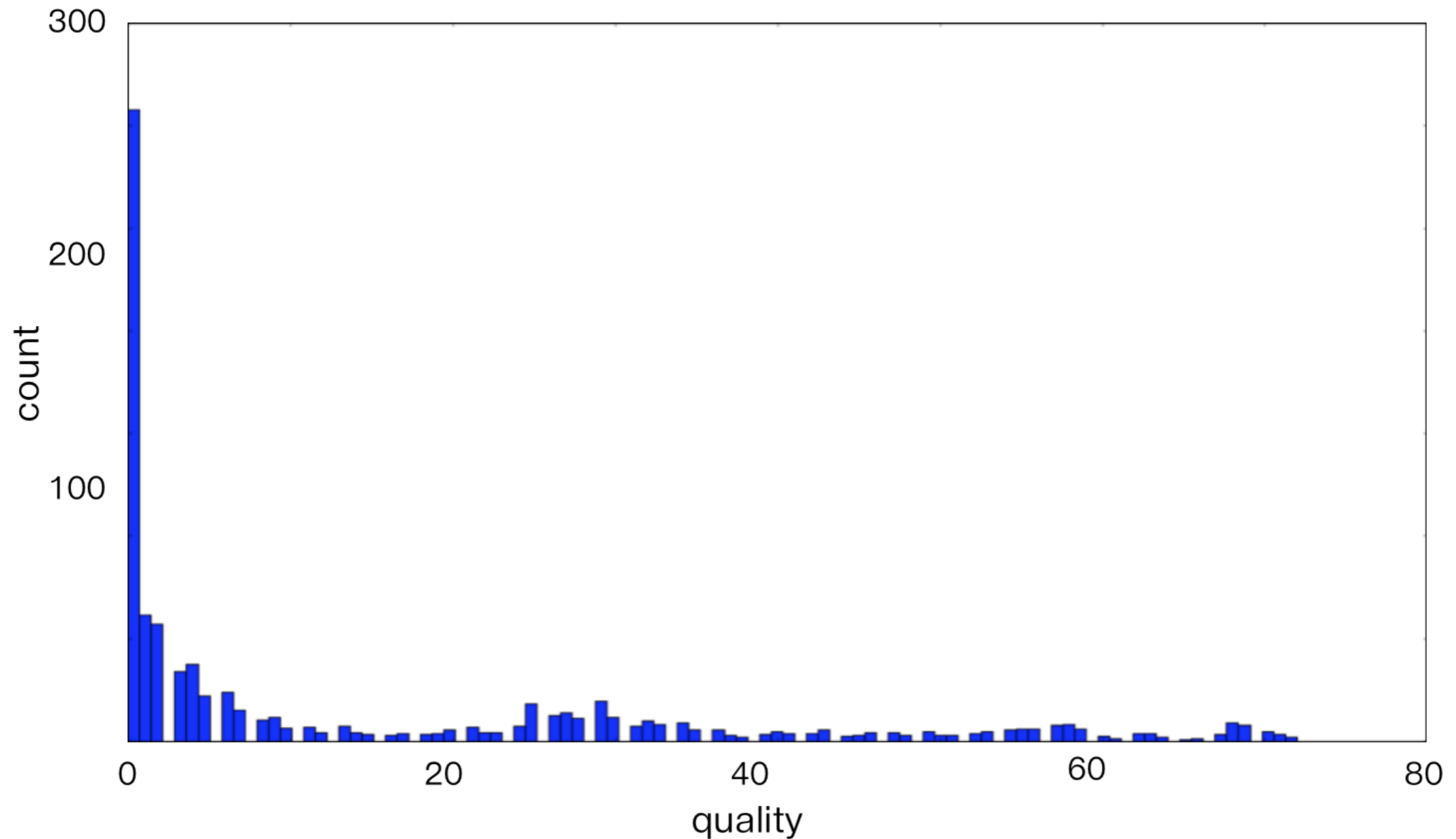
repeat N times

pick $w \in \mathbb{R}^n$ randomly

evaluate $\sum_{P_i} F(P_i, S_w(P_i))$

return best w found

Learning via Random Sampling



Bayesian Optimization

- A powerful method for solving difficult black-box optimization problems.
- Especially powerful when the objective function is expensive to evaluate.
- Key idea: use a probabilistic model to reduce the number of objective function evaluations.

Learning via Bayesian Optimization

repeat N times

select a promising w using the model

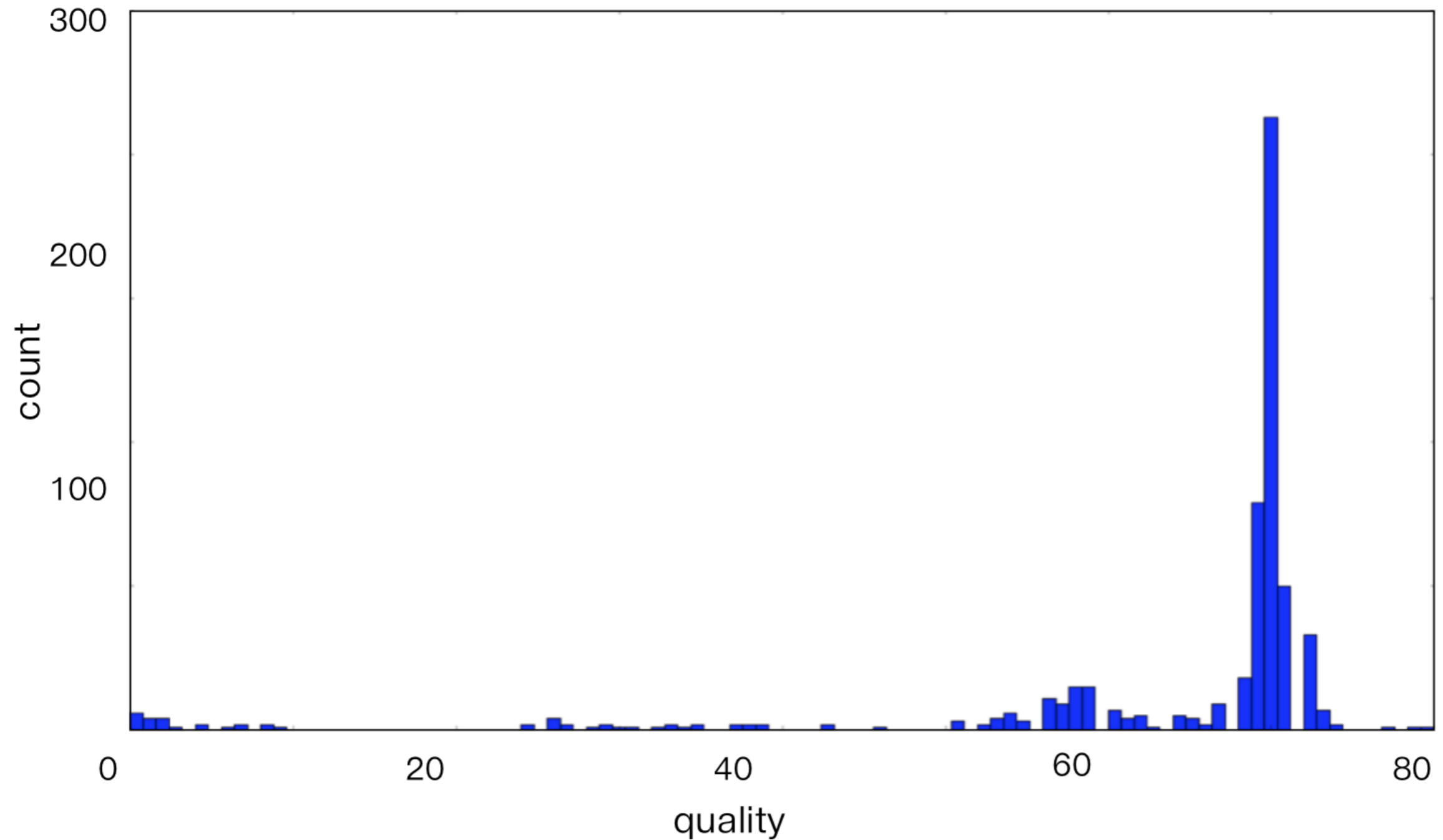
evaluate $\sum_{P_i} F(P_i, S_w(P_i))$

update the probabilistic model

return best w found

- Probabilistic model: Gaussian processes
- Selection strategy: Expected improvement

Learning via Bayesian Optimization

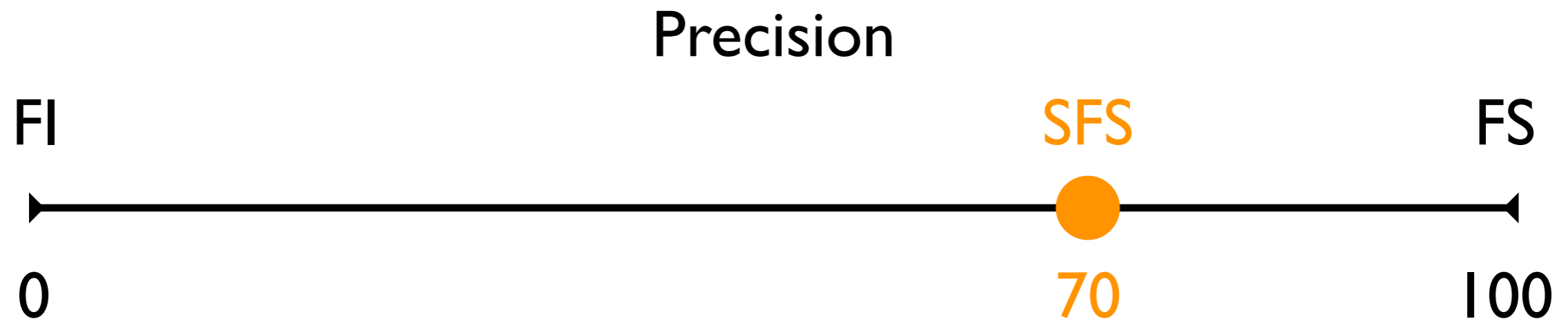


Effectiveness

- Implemented in Sparrow, an interval analyzer for C
- Evaluated on 30 open-source programs
 - 20 for training, 10 for testing

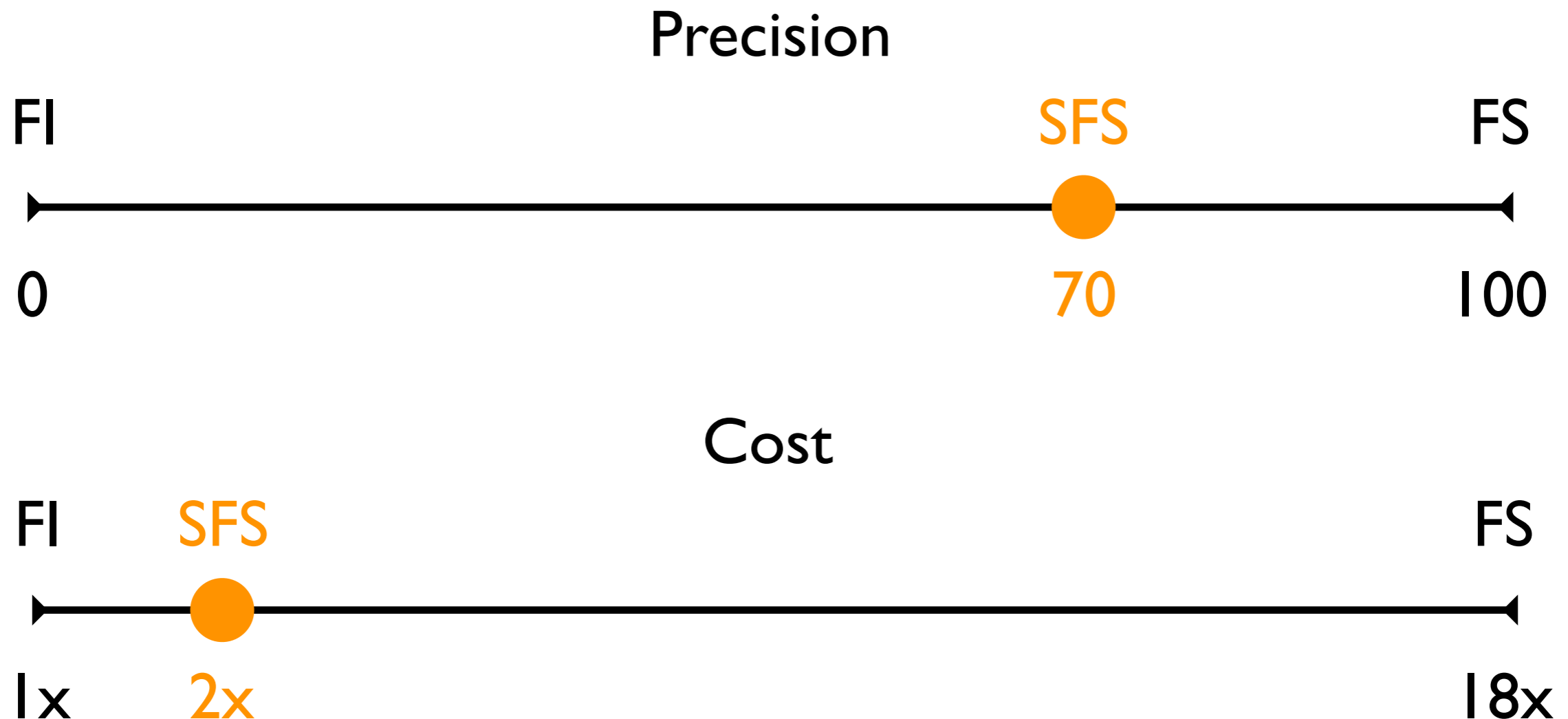
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- Implemented in Sparrow, an interval analyzer for C
- Evaluated on 30 open-source programs
 - 20 for training, 10 for testing



Limitations

- While promising, the method has limitations:
 - black-box optimization is inherently inefficient
 - manual feature engineering is needed
- Follow-up work to overcome the limitations:
 - improving the efficiency [APLAS'16, SAS'16]
 - automating feature engineering [on-going]

Improving Efficiency

- A white-box optimization method [APLAS'16]

$$\mathcal{O}_P : \mathbb{J}_P \rightarrow \mathbb{R}.$$

Find \mathbf{w}^* that minimizes $\sum_{j \in \mathbb{J}_P} (\text{score}_P^{\mathbf{w}}(j) - \mathcal{O}(j))^2$

- A supervised learning method [SAS'16]

| | a | -a | b | -b | c | -c | i | -i |
|----|---|----|---|----|---|----|---|----|
| a | ★ | ⊥ | ★ | ⊥ | ⊥ | ⊥ | ★ | ⊥ |
| -a | ⊥ | ★ | ⊥ | ★ | ⊥ | ⊥ | ⊥ | ⊥ |
| b | ★ | ⊥ | ★ | ⊥ | ⊥ | ⊥ | ★ | ⊥ |
| -b | ⊥ | ★ | ⊥ | ★ | ⊥ | ⊥ | ⊥ | ⊥ |
| c | ⊥ | ⊥ | ⊥ | ⊥ | ★ | ⊥ | ⊥ | ⊥ |
| -c | ⊥ | ⊥ | ⊥ | ⊥ | ⊥ | ★ | ⊥ | ⊥ |
| i | ⊥ | ⊥ | ⊥ | ⊥ | ⊥ | ⊥ | ★ | ⊥ |
| -i | ⊥ | ★ | ⊥ | ★ | ⊥ | ⊥ | ⊥ | ★ |

Manual Feature Engineering

- The success of ML heavily depends on the “features”
- Feature engineering is nontrivial and time-consuming
- Features do not generalize to other analyses

| Type | # | Features |
|------|----|---|
| A | 1 | local variable |
| | 2 | global variable |
| | 3 | structure field |
| | 4 | location created by dynamic memory allocation |
| | 5 | defined at one program point |
| | 6 | location potentially generated in library code |
| | 7 | assigned a constant expression (e.g., $x = c1 + c2$) |
| | 8 | compared with a constant expression (e.g., $x < c$) |
| | 9 | compared with an other variable (e.g., $x < y$) |
| | 10 | negated in a conditional expression (e.g., $!(x)$) |
| | 11 | directly used in malloc (e.g., $\text{malloc}(x)$) |
| | 12 | indirectly used in malloc (e.g., $y = x; \text{malloc}(y)$) |
| | 13 | directly used in realloc (e.g., $\text{realloc}(x)$) |
| | 14 | indirectly used in realloc (e.g., $y = x; \text{realloc}(y)$) |
| | 15 | directly returned from malloc (e.g., $x = \text{malloc}(e)$) |
| | 16 | indirectly returned from malloc |
| | 17 | directly returned from realloc (e.g., $x = \text{realloc}(e)$) |
| | 18 | indirectly returned from realloc |
| | 19 | incremented by one (e.g., $x = x + 1$) |
| | 20 | incremented by a constant expr. (e.g., $x = x + (1+2)$) |
| | 21 | incremented by a variable (e.g., $x = x + y$) |
| | 22 | decremented by one (e.g., $x = x - 1$) |
| | 23 | decremented by a constant expr (e.g., $x = x - (1+2)$) |
| | 24 | decremented by a variable (e.g., $x = x - y$) |
| | 25 | multiplied by a constant (e.g., $x = x * 2$) |
| | 26 | multiplied by a variable (e.g., $x = x * y$) |
| | 27 | incremented pointer (e.g., $p++$) |
| | 28 | used as an array index (e.g., $a[x]$) |
| | 29 | used in an array expr. (e.g., $x[e]$) |
| | 30 | returned from an unknown library function |
| | 31 | modified inside a recursive function |
| | 32 | modified inside a local loop |
| | 33 | read inside a local loop |
| B | 34 | $1 \wedge 8 \wedge (11 \vee 12)$ |
| | 35 | $2 \wedge 8 \wedge (11 \vee 12)$ |
| | 36 | $1 \wedge (11 \vee 12) \wedge (19 \vee 20)$ |
| | 37 | $2 \wedge (11 \vee 12) \wedge (19 \vee 20)$ |
| | 38 | $1 \wedge (11 \vee 12) \wedge (15 \vee 16)$ |
| | 39 | $2 \wedge (11 \vee 12) \wedge (15 \vee 16)$ |
| | 40 | $(11 \vee 12) \wedge 29$ |
| | 41 | $(15 \vee 16) \wedge 29$ |
| | 42 | $1 \wedge (19 \vee 20) \wedge 33$ |
| | 43 | $2 \wedge (19 \vee 20) \wedge 33$ |
| | 44 | $1 \wedge (19 \vee 20) \wedge \neg 33$ |
| | 45 | $2 \wedge (19 \vee 20) \wedge \neg 33$ |

flow-sensitivity

| Type | # | Features |
|------|----|--|
| A | 1 | leaf function |
| | 2 | function containing malloc |
| | 3 | function containing realloc |
| | 4 | function containing a loop |
| | 5 | function containing an if statement |
| | 6 | function containing a switch statement |
| | 7 | function using a string-related library function |
| | 8 | write to a global variable |
| | 9 | read a global variable |
| | 10 | write to a structure field |
| | 11 | read from a structure field |
| | 12 | directly return a constant expression |
| | 13 | indirectly return a constant expression |
| | 14 | directly return an allocated memory |
| | 15 | indirectly return an allocated memory |
| | 16 | directly return a reallocated memory |
| | 17 | indirectly return a reallocated memory |
| | 18 | return expression involves field access |
| | 19 | return value depends on a structure field |
| | 20 | return void |
| | 21 | directly invoked with a constant |
| | 22 | constant is passed to an argument |
| | 23 | invoked with an unknown value |
| | 24 | functions having no arguments |
| | 25 | functions having one argument |
| | 26 | functions having more than one argument |
| | 27 | functions having an integer argument |
| | 28 | functions having a pointer argument |
| | 29 | functions having a structure as an argument |
| B | 30 | $2 \wedge (21 \vee 22) \wedge (14 \vee 15)$ |
| | 31 | $2 \wedge (21 \vee 22) \wedge \neg(14 \vee 15)$ |
| | 32 | $2 \wedge 23 \wedge (14 \vee 15)$ |
| | 33 | $2 \wedge 23 \wedge \neg(14 \vee 15)$ |
| | 34 | $2 \wedge (21 \vee 22) \wedge (16 \vee 17)$ |
| | 35 | $2 \wedge (21 \vee 22) \wedge \neg(16 \vee 17)$ |
| | 36 | $2 \wedge 23 \wedge (16 \vee 17)$ |
| | 37 | $2 \wedge 23 \wedge \neg(16 \vee 17)$ |
| | 38 | $(21 \vee 22) \wedge \neg 23$ |

context-sensitivity

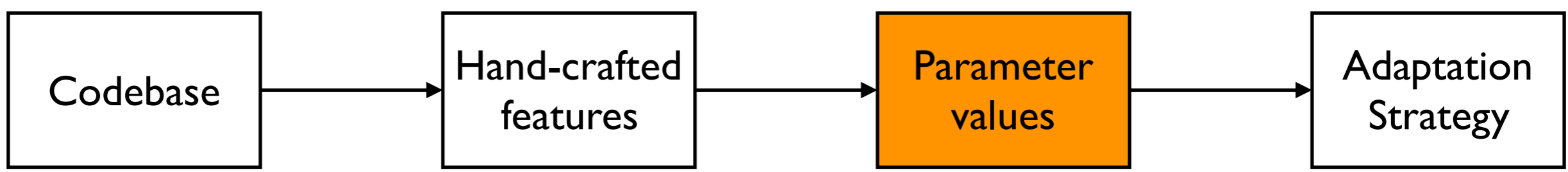
| Type | # | Features |
|------|----|--|
| A | 1 | used in array declarations (e.g., $a[c]$) |
| | 2 | used in memory allocation (e.g., $\text{malloc}(c)$) |
| | 3 | used in the righthand-side of an assignment (e.g., $x = c$) |
| | 4 | used with the less-than operator (e.g., $x < c$) |
| | 5 | used with the greater-than operator (e.g., $x > c$) |
| | 6 | used with \leq (e.g., $x \leq c$) |
| | 7 | used with \geq (e.g., $x \geq c$) |
| | 8 | used with the equality operator (e.g., $x == c$) |
| | 9 | used with the not-equality operator (e.g., $x != c$) |
| | 10 | used within other conditional expressions (e.g., $x < c + y$) |
| | 11 | used inside loops |
| | 12 | used in return statements (e.g., $\text{return } c$) |
| | 13 | constant zero |
| B | 14 | $(1 \vee 2) \wedge 3$ |
| | 15 | $(1 \vee 2) \wedge (4 \vee 5 \vee 6 \vee 7)$ |
| | 16 | $(1 \vee 2) \wedge (8 \vee 9)$ |
| | 17 | $(1 \vee 2) \wedge 11$ |
| | 18 | $(1 \vee 2) \wedge 12$ |
| | 19 | $13 \wedge 3$ |
| | 20 | $13 \wedge (4 \vee 5 \vee 6 \vee 7)$ |
| | 21 | $13 \wedge (8 \vee 9)$ |
| | 22 | $13 \wedge 11$ |
| | 23 | $13 \wedge 12$ |

widening thresholds

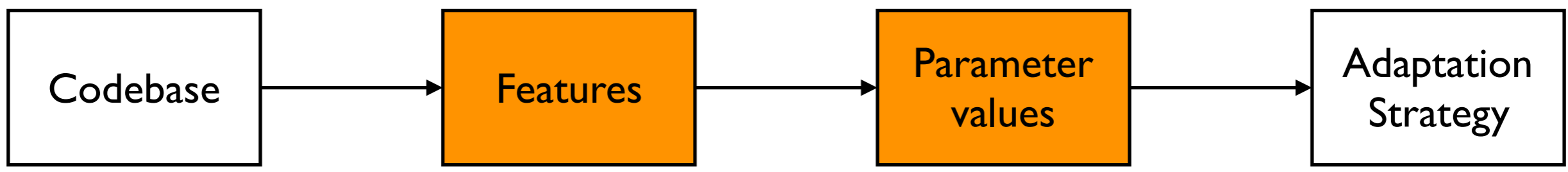
on-going

Automating Feature Engineering

Before [OOPSLA'15,SAS'16,APLAS'16]



New method



on-going

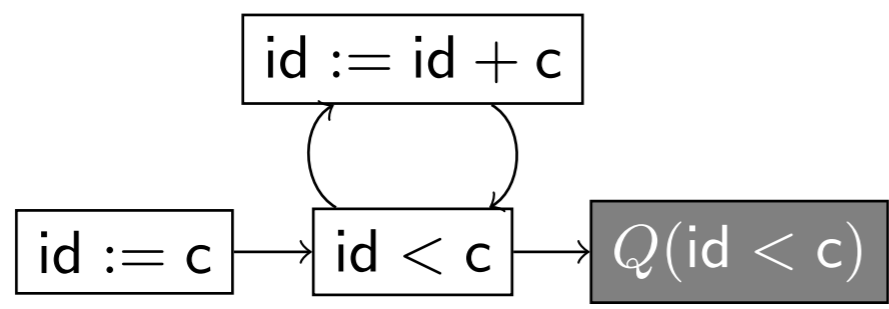
Key Ideas

- Use a program reducer to generate *feature programs* that capture the key reason why FS succeeds but FI fails.

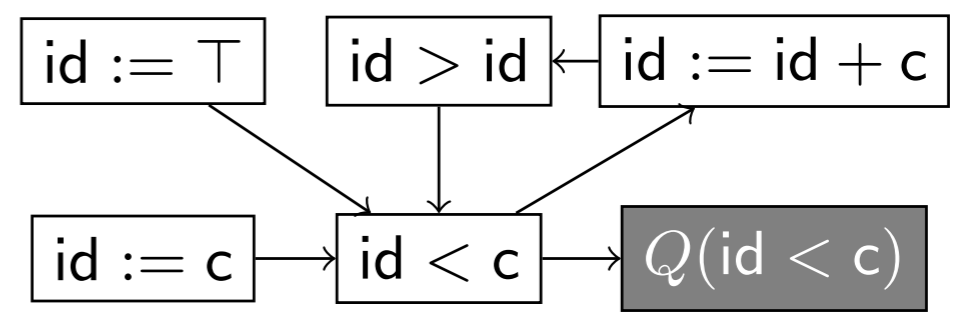
```
int j = 0;
main() {
  j++;
  assert (j>0);
}
```

```
main() {
  for (int i=1; i<50; i++) {
    assert (i<100);
  }
}
```

- Generalize the programs by abstract data flow graphs



?
∪



Summary

- Challenges in selective static analysis
- Using machine learning is promising
 - [OOPSLA'15, SAS'16, APLAS'16,...]
 - flow-sensitivity, context-sensitivity, relational domain, widening thresholds, soundness, etc
- Generally applicable beyond static analysis
 - e.g., concolic testing

Summary

- Challenges in selective static analysis
- Using machine learning is promising
 - [OOPSLA'15, SAS'16, APLAS'16,...]
 - flow-sensitivity, context-sensitivity, relational domain, widening thresholds, soundness, etc
- Generally applicable beyond static analysis
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Thank you