#### Introduction to Software Research @Korea University

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#### **Research Goals**

 Computer-aided software engineering: automated programming / testing / debugging



#### **Data-Driven Program Analysis**

### Heuristics in Program Analysis



- Practical program analysis tools use many heuristics
  - E.g., context/flow-sensitivity, variable clustering, unsoundness, trace partitioning, path selection/pruning, state merging, etc
- Developing a good heuristic is an art
  - Manually done by analysis designers: nontrivial & suboptimal

# Automatically Generating Analysis Heuristics from Data

 Use data to make heuristic decisions in program analysis



context-sensitivity heuristics flow-sensitivity heuristics unsoundness heuristics path-selection heuristics

- Automatic: little reliance on analysis designers
- Powerful: machine-tuning outperforms hand-tuning
- Stable: can be tuned for target programs

#### **Context-Sensitivity**

```
class D{} class E{}
1:
2:
3:
   class C{
   Object id(Object v){return v;}}
4:
5:
   class B{
6:
   void dummy(){}
7:
   Object id(Object v){
8:
   C c = new C(); //C1
9:
10: return c.id(v);}}
11:
12: class A{
13: public static void main(String[] args){
14: B b1 = new B(); //B1
15: B b2 = new B(); //B2
16: D d = (D) b1.id1(new D());//query1
17: E e = (E) b2.id1(new E());//query2
18: b1.dummy();
19: b2.dummy();}}
```

Without context-sensitivity, analysis fails to prove queries



#### **Context-Sensitivity**

```
class D{} class E{}
1:
2:
3:
   class C{
   Object id(Object v){return v;}}
4:
5:
6: class B{
7: void dummy(){}
   Object id(Object v){
8:
   C c = new C(); //C1
9:
10: return c.id(v);}}
11:
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14: B b1 = new B();//B1
15: B b2 = new B(); //B2
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17: E e = (E) b2.id1(new E());//query2
18: b1.dummy();
19: b2.dummy();}}
```

#### 2-object-sensitivity succeeds but does not scale



### Selective Context-Sensitivity

```
class D{} class E{}
1:
2:
3:
   class C{
   Object id(Object v){return v;}}
4:
5:
   class B{
6:
  void dummy(){}
7:
  Object id(Object v){
8:
  C c = new C();//C1
9:
10: return c.id(v);}}
11:
12: class A{
13: public static void main(String[] args){
14: B b1 = new B(); //B1
15: B b2 = new B(); //B2
16: D d = (D) b1.id1(new D());//query1
17: E = (E) b2.id1(new E());//query2
18: b1.dummy();
19: b2.dummy();}}
```

Apply 2-obj-sens: {C.id} Apply 1-obj-sens: {B.id} Apply insens: {B.m}



### Selective Context-Sensitivity

```
class D{} class E{}
1:
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3:
   class C{
   Object id(Object v){return v;}}
4:
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   class B{
6:
  void dummy(){}
7:
  Object id(Object v){
8:
  C c = new C();//C1
9:
10: return c.id(v);}}
11:
12: class A{
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16: D d = (D) b1.id1(new D());//query1
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18: b1.dummy();
19: b2.dummy();}}
```

Apply 2-obj-sens: {C.id} Apply 1-obj-sens: {B.id} Apply insens: {B.m}



Challenge: How to decide? Data-driven approach

# OPD Our Data-Driven Approach



# OPD Our Data-Driven Approach



Heuristic for applying (hybrid) object-sensitivity:

#### f2: Methods that require 2-object-sensitivity

 $1 \wedge \neg 3 \wedge \neg 6 \wedge 8 \wedge \neg 9 \wedge \neg 16 \wedge \neg 17 \wedge \neg 18 \wedge \neg 19 \wedge \neg 20 \wedge \neg 21 \wedge \neg 22 \wedge \neg 23 \wedge \neg 24 \wedge \neg 25$ 

#### fl: Methods that require 1-object-sensitivity

 $\begin{array}{l} (1 \land \neg 3 \land \neg 4 \land \neg 7 \land \neg 8 \land 6 \land \neg 9 \land \neg 15 \land \neg 16 \land \neg 17 \land \neg 18 \land \neg 19 \land \neg 20 \land \neg 21 \land \neg 22 \land \neg 23 \land \neg 24 \land \neg 25) \lor \\ (\neg 3 \land \neg 4 \land \neg 7 \land \neg 8 \land \neg 9 \land 10 \land 11 \land 12 \land 13 \land \neg 16 \land \neg 17 \land \neg 18 \land \neg 19 \land \neg 20 \land \neg 21 \land \neg 22 \land \neg 23 \land \neg 24 \land \neg 25) \lor \\ (\neg 3 \land \neg 9 \land 13 \land 14 \land 15 \land \neg 16 \land \neg 17 \land \neg 18 \land \neg 19 \land \neg 20 \land \neg 21 \land \neg 22 \land \neg 23 \land \neg 24 \land \neg 25) \lor \\ (1 \land 2 \land \neg 3 \land 4 \land \neg 5 \land \neg 6 \land \neg 7 \land \neg 8 \land \neg 9 \land \neg 10 \land \neg 13 \land \neg 15 \land \neg 16 \land \neg 17 \land \neg 18 \land \neg 19 \land \neg 20 \land \neg 21 \land \neg 22 \land \neg 24 \land \neg 25) \lor \\ (\neg 23 \land \neg 24 \land \neg 5 \land \neg 6 \land \neg 7 \land \neg 8 \land \neg 9 \land \neg 10 \land \neg 13 \land \neg 15 \land \neg 16 \land \neg 17 \land \neg 18 \land \neg 19 \land \neg 20 \land \neg 21 \land \neg 22 \land \neg 24 \land \neg 25) \lor \\ \end{array}$ 

#### Performance

- Training with 4 small programs from DaCapo, and applied to 6 large programs (I for validation)
- Machine-tuning outperforms hand-tuning



#### **Other Context-Sensitivities**

#### • Plain (not hybrid) Object-sensitivity:

- Depth-2 formula  $(f_2)$ :

 $1 \wedge \neg 3 \wedge \neg 6 \wedge 8 \wedge \neg 9 \wedge \neg 16 \wedge \neg 17 \wedge \neg 18 \wedge \neg 19 \wedge \neg 20 \wedge \neg 21 \wedge \neg 22 \wedge \neg 23 \wedge \neg 24 \wedge \neg 25$ 

– Depth-1 formula  $(f_1)$ :

 $(1 \land 2 \land \neg 3 \land \neg 6 \land \neg 7 \land \neg 8 \land \neg 9 \land \neg 16 \land \neg 17 \land \neg 18 \land \neg 19 \land \neg 20 \land \neg 21 \land \neg 22 \land \neg 23 \land \neg 24 \land \neg 25) \lor (\neg 1 \land \neg 2 \land 5 \land 8 \land \neg 9 \land 11 \land 12 \land \neg 14 \land \neg 15 \land \neg 16 \land \neg 17 \land \neg 18 \land \neg 19 \land \neg 20 \land \neg 21 \land \neg 22 \land \neg 23 \land \neg 24 \land \neg 25) \lor (\neg 3 \land \neg 4 \land \neg 7 \land \neg 8 \land \neg 9 \land 10 \land 11 \land 12 \land \neg 16 \land \neg 17 \land \neg 18 \land \neg 19 \land \neg 20 \land \neg 21 \land \neg 22 \land \neg 23 \land \neg 24 \land \neg 25)$ 

#### • Call-site-sensitivity:

– Depth-2 formula  $(f_2)$ :

 $1 \wedge \neg 6 \wedge \neg 7 \wedge 11 \wedge 12 \wedge 13 \wedge \neg 16 \wedge \neg 17 \wedge \neg 18 \wedge \neg 19 \wedge \neg 20 \wedge \neg 21 \wedge \neg 22 \wedge \neg 23 \wedge \neg 24 \wedge \neg 25$ 

– Depth-1 formula  $(f_1)$ :

 $(1 \land 2 \land \neg 7 \land \neg 16 \land \neg 17 \land \neg 18 \land \neg 19 \land \neg 20 \land \neg 21 \land \neg 22 \land \neg 23 \land \neg 24 \land \neg 25)$ 

#### • Type-sensitivity:

- Depth-2 formula  $(f_2)$ :

 $1 \wedge \neg 3 \wedge \neg 6 \wedge 8 \wedge \neg 9 \wedge \neg 16 \wedge \neg 17 \wedge \neg 18 \wedge \neg 19 \wedge \neg 20 \wedge \neg 21 \wedge \neg 22 \wedge \neg 23 \wedge \neg 24 \wedge \neg 25$ 

– Depth-1 formula  $(f_1)$ :

$$1 \land 2 \land \neg 3 \land \neg 6 \land \neg 7 \land \neg 8 \land \neg 9 \land \neg 15 \land \neg 16 \land \neg 17 \land \neg 18 \land \neg 19 \land \neg 20 \land \neg 21 \land \neg 22 \land \neg 23 \land \neg 24 \land \neg 25$$

## **Obj-Sens vs. Type-Sens**

- In theory, obj-sens is more precise than type-sens
- The set of methods that benefit from obj-sens is a superset of the methods that benefit from type-sens
- Interestingly, our algorithm automatically discovered this rule from data:

<i>f</i> <sub>1</sub> for <i>20bjH+Data</i>	•	$(1 \land 2 \land \neg 3 \land \neg 6 \land \neg 7 \land \neg 8 \land \neg 9 \land \neg 16 \land \cdots \land \neg 22 \land \neg 23 \land \neg 24 \land \neg 25) \lor (\neg 1 \land \neg 2 \land 8 \land 5 \land \neg 9 \land 11 \land 12 \land \cdots \land \neg 21 \land \neg 22 \land \neg 23 \land \neg 24 \land \neg 25) \lor (\neg 3 \land \neg 4 \land \neg 7 \land \neg 8 \land \neg 9 \land 10 \land 11 \land \cdots \land \neg 21 \land \neg 22 \land \neg 23 \land \neg 24 \land \neg 25)$
f <sub>1</sub> for 2typeH+Data	•	$1 \land 2 \land \neg 3 \land \neg 6 \land \neg 7 \land \neg 8 \land \neg 9 \land \neg 15 \land \neg 16 \land \cdots \land \neg 22 \land \neg 23 \land \neg 24 \land \neg 25$

# Concolic Testing (Dynamic Symbolic Execution)

• Concolic testing is an effective software testing method based on symbolic execution



- Key challenge: path explosion
- Our solution: mitigate the problem with good search heuristics

#### Limitation of Random Testing

```
int double (int v) {
   return 2*v;
}
```

void testme(int x, int y) {

```
z := double (y);
```

```
if (z==x) {
```

Probability of the error? ( $0 \le x, y \le 100$ )

#### Limitation of Random Testing

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int double (int v) {
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Probability of the error?  $(0 \le x, y \le 100)$ 

< 0.4%

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```

```
if (z==x) {
```

Probability of the error?  $(0 \le x, y \le 100)$ 

< 0.4%

- random testing requires 250 runs
- concolic testing finds it in 3 runs



lst iteration









2nd iteration



















execution tree

### **Concolic Testing** $b_1$ b solve $(\neg b_1)$ **b**4 b **b**5 Ф2

execution tree



execution tree

## **Concolic Testing Algorithm**

**Input** :Program *P*, initial input vector  $v_0$ , budget *N* **Output**:The number of branches covered

1: 
$$T \leftarrow \langle \rangle$$

2: 
$$v \leftarrow v_0$$

3: **for** 
$$m = 1$$
 to  $N$  **do**

4: 
$$\Phi_m \leftarrow \text{RunProgram}(P, v)$$

5: 
$$T \leftarrow T \cdot \Phi_m$$

#### 6: repeat

7: 
$$(\Phi, \phi_i) \leftarrow \text{Choose}(T) \qquad (\Phi = \phi_1 \land \cdots \land \phi_n)$$

8: **until** SAT
$$(\bigwedge_{j < i} \phi_j \land \neg \phi_i)$$

9: 
$$v \leftarrow \operatorname{model}(\bigwedge_{j < i} \phi_j \land \neg \phi_i)$$

10: **end for** 

11: **return** |Branches(T)|

## **Concolic Testing Algorithm**

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Search Heuristic

6: repeat

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$$v \leftarrow \operatorname{model}(\bigwedge_{j < i} \phi_j \land \neg \phi_i)$$

10: **end for** 

11: **return** |Branches(T)|

#### Search Heuristics

- Concolic testing relies on search heuristics to maximize code coverage in a limited time budget.
- Key but the most manual and ad-hoc component of concolic testing
- Numerous heuristics have been proposed:
  - DFS [PLDI'05], BFS, Random, CFDS [ASE'08], Generational [NDSS'08], CarFast[FSE'12], CGS [FSE'14], ...

#### Limitations of Existing Search Heuristics

- No existing heuristics perform well in practice
- Developing a heuristic requires a huge amount of engineering effort and expertise.



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Our goal: automatically generating search heuristics

### **Effectiveness of Our Method**

• Considerable increase in branch coverage

1CSE'18



# Effectiveness of Our Method

• Considerable increase in branch coverage



• Dramatic increase in bug-finding

	OURS	CFDS	CGS	Random	Gen	DFS
gawk-3.0.3	100/100	0/100	0/100	0/100	0/100	0/100
grep-2.2	47/100	0/100	5/100	0/100	0/100	0/100

### Automatic Debugging (Automatic Program Repair)

#### MemFix: 메모리 관리 오류 자동 수정기

• 메모리 관리 오류: C/C++에서 빈번하게 발생



• 심각한 소프트웨어 보안취약점의 주요 원인



• 사전 탐지 및 정확한 수정이 매우 어려움

```
in = malloc(1);
out = malloc(1);
... // use in, out
free(out);
free(in);
in = malloc(2);
if (in == NULL) {
  goto err;
}
out = malloc(2);
if (out == NULL) {
  free(in);
  goto err;
}
... // use in, out
err:
  free(in);
  free(out);
  return;
```

```
in = malloc(1);
             out = malloc(1);
              ... // use in, out
              free(out);
              free(in);
              in = malloc(2);
             if (in == NULL) {
               goto err;
             }
             out = malloc(2);
              if (out == NULL) {
                free(in);
               goto err;
              }
              ... // use in, out
             err:
               free(in);
double-free
                free(out);
                return;
```

```
in = malloc(1);
              out = malloc(1);
              ... // use in, out
              free(out);
              free(in);
              in = malloc(2);
              if (in == NULL) {
                goto err;
              }
              out = malloc(2);
              if (out == NULL) {
                free(in);
               goto err;
double-free ( ... // use in, out err:
                free(in);
                free(out);
                return;
```

#### USB: fix double frees in error code paths of ipaq driver

the error code paths can be enter with buffers to freed buffers. Serial core would do a kfree() on memory already freed.

Signed-off-by: Oliver Neukum <oneukum@suse.de>
Signed-off-by: Greg Kroah-Hartman <gregkh@suse.de>

P master V4.15-rc1 --- v2.6.24-rc1

Oliver Neukum committed with gregkh on 18 Sep 2007

```
in = malloc(1);
out = malloc(1);
... // use in, out
free(out);
free(in);
```

```
in = malloc(2);
if (in == NULL) {
    out = NULL;
    goto err;
}
```

```
out = malloc(2);
if (out == NULL) {
   free(in);
   in = NULL;
   goto err;
}
... // use in, out
err:
   free(in);
   free(out);
   return;
```

1 par

#### USB: fix double kfree in ipaq in error case

in the error case the ipaq driver leaves a dangling pointer to already freed memory that will be freed again.

Signed-off-by: Oliver Neukum <oneukum@suse.de>
Signed-off-by: Greg Kroah-Hartman <gregkh@suse.de>

```
P master > v4.15-rc1 ... v2.6.27-rc1
```

Oliver Neukum committed with gregkh on 30 Jun 2008

```
1 parent 35
```

```
in = malloc(1);
out = malloc(1);
... // use in, out
// removed
free(in);
in = malloc(2);
if (in == NULL) {
  out = NULL;
  goto err;
}
free(out);
out = malloc(2);
if (out == NULL) {
  free(in);
  in = NULL;
  goto err;
}
... // use in, out
err:
  free(in);
  free(out);
  return;
```

```
in = malloc(1);
out = malloc(1);
... // use in, out
// removed
free(in);
in = malloc(2);
if (in == NULL) {
  out = NULL;
  goto err;
}
free(out);
out = malloc(2);
if (out == NULL) {
  free(in);
  in = NULL;
  goto err;
}
... // use in, out
err:
  free(in);
  free(out);
  return;
```

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P master V4.15-rc1 v2.6.27-rc1

Oliver Neukum committed with gregkh on 30 Jun 2008

1 parent 35

memory lea

#### fix for a memory leak in an error case introduced by fix for double free

The fix NULLed a pointer without freeing it.

Signed-off-by: Oliver Neukum <oneukum@suse.de> Reported-by: Juha Motorsportcom <juha\_motorsportcom@luukku.com> Signed-off-by: Linus Torvalds <torvalds@linux-foundation.org>

P master V4.15-rc1 v2.6.27-rc1

Oliver Neukum committed with torvalds on 27 Jul 2008

1 parent 9ee08c2

```
in = malloc(1);
out = malloc(1);
... // use in, out
free(out);
free(in);
out = NULL;
in = malloc(2);
if (in == NULL) {
  out = NULL;
  goto err;
}
// removed
out = malloc(2);
if (out == NULL) {
  free(in);
  in = NULL;
  goto err;
}
... // use in, out
err:
  free(in);
  free(out);
  return;
```

```
in = malloc(1);
out = malloc(1);
... // use in, out
free(out);
free(in);
in = malloc(2);
if (in == NULL) {
  goto err;
                            MemFix
}
out = malloc(2);
if (out == NULL) {
  free(in);
  goto err;
}
... // use in, out
err:
  free(in);
  free(out);
  return;
```

in = malloc(1);out = malloc(1); ... // use in, out // removed free(in); in = malloc(2);if (in == NULL) { goto err; } free(out); out = malloc(2); if (out == NULL) { // removed goto err; } ... // use in, out err: free(in); free(out); return;

## MemFix 알고리즘



(undecidable)

FSE'18

(NP-complete)

(NP-complete)

### MemFix 알고리즘

- Soundness and safety proved formally
  - Soundness: the patch gurantees to fix the error
  - Safety: no new errors are introduced

#### Automatic Feedback Generation for Programming Assignments

- In my programming language course,
  - students hardly receive personalized feedback, and
  - instructor's solutions are not very helpful.

모범 답안	오답 코드
<pre>let rec map f (l,var) =     match l with     [] -&gt; []       hd::tl -&gt; (f (hd,var))::(map f (tl,var))   Sum lst -&gt; Sum (map diff (lst,var))</pre>	   Sum plus -> Sum (match plus with [] -> Const 0   [hd] -> diff( hd, var)   hd::tl -> Sum [diff(hd, var); diff(Times tl, var)] )

#### 학생 제출 답안

| \_ -> result



type aexp = ( |CONST of int | VAR of string | POWER of string \* int | TIMES of aexp list | SUM of aexp list type env = (string \* int \* int) list let diff : aexp \* string -> aexp | \_ -> = fun (aexp, x) -> let rec deployEnv : env -> int -> aexp list = fun env flag -> ) match env with | hd::tl -> ) ( match hd with in |(x, c, p) -> if (flag = 0 && c = 0) then deployEnv tl flag else if (x = "const" && flag = 1 && c = 1) then deployEnv tl flag else if (p = 0) then (CONST c)::(deployEnv tl flag) match aexp with else if (c = 1 && p = 1) then (VAR x)::(deployEnv tl flag) | SUM 1st -> else if (p = 1) then TIMES[CONST c; VAR x]::(deployEnv tl flag) ( else if (c = 1) then POWER(x, p)::(deployEnv tl flag) match 1st with else TIMES [CONST c; POWER(x, p)]::(deployEnv tl flag) ) | [] -> [] in let rec updateEnv : (string \* int \* int) -> env -> int -> env = fun elem env flag -> match env with | (hd::tl) -> | h::t -> ( match hd with | (x, c, p) -> ( ) match elem with |(x2, c2, p2) -> ) if (flag = 0) then | TIMES lst -> if (x = x2 && p = p2) then (x, (c + c2), p)::tl ( else hd::(updateEnv elem tl flag) match 1st with else if (x = x2) then (x, (c\*c2), (p + p2))::tl else hd::(updateEnv elem tl flag) ) ) | [] -> elem::[] in | h::t -> let rec doDiff : aexp \* string -> aexp = fun (aexp, x) -> match aexp with | CONST \_ -> CONST 0 ) | VAR v -> if (x = v) then CONST 1 else CONST 0 ) | POWER (v, p) -> in if (p = 0) then CONST 0 else if (x = v) then TIMES ((CONST p)::POWER (v, p-1)::[]) else CONST 0 match result with | TIMES lst -> (

match 1st with

```
match (hd, diff_hd, tl, diff_tl) with
          | (CONST p, CONST s, [CONST r], CONST q) -> CONST (p*q + r*s)
           | (CONST p, _, _, CONST q) ->
             if (diff_hd = CONST 0 || tl = [CONST 0]) then CONST (p*q)
             else SUM [CONST(p*q); TIMES(diff_hd::tl)]
           | (_, CONST s, [CONST r], _) ->
             if (hd = CONST 0 || diff_tl = CONST 0) then CONST (r*s)
             else SUM [TIMES [hd; diff_tl]; CONST(r*s)]
             if (hd = CONST 0 || diff_tl = CONST 0) then TIMES(diff_hd::tl)
             else if (tl = [CONST 0] || diff_hd = CONST 0) then TIMES [hd; diff_tl]
             else SUM [TIMES [hd; diff_tl]; TIMES (diff_hd::tl)]
     | [] -> CONST 0
| SUM lst -> SUM(List.map (fun aexp -> doDiff(aexp, x)) lst)
let rec simplify : aexp -> env -> int -> aexp list
= fun aexp env flag ->
     | (CONST c)::tl -> simplify (SUM tl) (updateEnv ("const", c, 0) env 0) 0
     | (VAR x)::tl -> simplify (SUM tl) (updateEnv (x, 1, 1) env 0) 0
     (POWER (x, p))::tl -> simplify (SUM tl) (updateEnv (x, 1, p) env 0) 0
     | (SUM lst)::tl -> simplify (SUM (List.append lst tl)) env 0
     | (TIMES lst)::tl ->
          let l = simplify (TIMES lst) [] 1 in
          match 1 with
             if (t = []) then List.append l (simplify (SUM tl) env 0)
             else List.append (TIMES 1::[]) (simplify (SUM tl) env 0)
          | [] -> []
     | [] -> deployEnv env 0
     | (CONST c)::tl -> simplify (TIMES tl) (updateEnv ("const", c, 0) env 1) 1
     | (VAR x)::tl -> simplify (TIMES tl) (updateEnv (x, 1, 1) env 1) 1
     | (POWER (x, p))::tl -> simplify (TIMES tl) (updateEnv (x, 1, p) env 1) 1
     | (SUM lst)::tl ->
          let 1 = simplify (SUM 1st) [] 0 in
          match 1 with
             if (t = []) then List.append l (simplify (TIMES tl) env 1)
              else List.append (SUM 1::[]) (simplify (TIMES tl) env 1)
           [] -> [] (* Feedback : Replace [] by ((Sum lst) :: tl) *)
      | (TIMES lst)::tl -> simplify (TIMES (List.append lst tl)) env 1
     | [] -> deployEnv env 1
let result = doDiff (aexp, x) in
| SUM _ -> SUM (simplify result [] 0)
| TIMES _ -> TIMES (simplify result [] 1)
```

```
let rec diff : aexp * string -> aexp
= fun (e, x) ->
match e with
| Const n -> Const 0
| Var a -> if (a <> x) then Const 0 else Const 1
| Power (a, n) -> if (a <> x) then Const 0 else Times [Const n; Power (a, n-1)]
| Times 1 ->
begin
match 1 with
| [] -> Const 0
| hd::tl -> Sum [Times ((diff (hd, x))::tl); Times [hd; diff (Times tl, x)]]
end
| Sum 1 -> Sum (List.map (fun e -> diff (e,x)) 1)
```

#### 학생 제출 답안

#### 모범답안

let rec diff : aexp \* string -> aexp type aexp = ( = fun (e, x) -> |CONST of int match (hd, diff\_hd, tl, diff\_tl) with match e with | VAR of string | (CONST p, CONST s, [CONST r], CONST q) -> CONST (p\*q + r\*s) | Const n -> Const 0 | POWER of string \* int | (CONST p, \_, \_, CONST q) -> | Var a -> if (a <> x) then Const 0 else Const 1 | TIMES of aexp list if (diff\_hd = CONST 0 || tl = [CONST 0]) then CONST (p\*q) | Power (a, n)  $\rightarrow$  if (a > x) then Const 0 else Times [Const n; Power (a, n-1)] | SUM of aexp list else SUM [CONST(p\*q); TIMES(diff\_hd::tl)] | Times 1 -> | (\_, CONST s, [CONST r], \_) -> begin type env = (string \* int \* int) list if (hd = CONST 0 || diff\_tl = CONST 0) then CONST (r\*s) match 1 with else SUM [TIMES [hd; diff\_tl]; CONST(r\*s)] | [] -> Const 0 let diff : aexp \* string -> aexp | \_ -> | hd::tl -> Sum [Times ((diff (hd, x))::tl); Times [hd; diff (Times tl, x)]] = fun (aexp, x) -> if (hd = CONST 0 || diff\_tl = CONST 0) then TIMES(diff\_hd::tl) end else if (tl = [CONST 0] || diff\_hd = CONST 0) then TIMES [hd; diff\_tl] | Sum 1 -> Sum (List.map (fun e -> diff (e,x)) 1) let rec deployEnv : env -> int -> aexp list else SUM [TIMES [hd; diff\_tl]; TIMES (diff\_hd::tl)] = fun env flag -> ) match env with | [] -> CONST 0 | hd::tl -> ) ( | SUM lst -> SUM(List.map (fun aexp -> doDiff(aexp, x)) lst) match hd with in |(x, c, p) -> if (flag = 0 && c = 0) then deployEnv tl flag let rec simplify : aexp -> env -> int -> aexp list else if (x = "const" && flag = 1 && c = 1) then deployEnv tl flag = fun aexp env flag -> else if (p = 0) then (CONST c)::(deployEnv tl flag) match aexp with else if (c = 1 && p = 1) then (VAR x)::(deployEnv tl flag) | SUM 1st -> else if (p = 1) then TIMES[CONST c; VAR x]::(deployEnv tl flag) ( else if (c = 1) then POWER(x, p)::(deployEnv tl flag) match 1st with else TIMES [CONST c; POWER(x, p)]::(deployEnv tl flag) | (CONST c)::tl -> simplify (SUM tl) (updateEnv ("const", c, 0) env 0) 0 ) | (VAR x)::tl -> simplify (SUM tl) (updateEnv (x, 1, 1) env 0) 0 | [] -> [] (POWER (x, p))::tl -> simplify (SUM tl) (updateEnv (x, 1, p) env 0) 0 in | (SUM lst)::tl -> simplify (SUM (List.append lst tl)) env 0 | (TIMES lst)::tl -> let rec updateEnv : (string \* int \* int) -> env -> int -> env = fun elem env flag -> let l = simplify (TIMES lst) [] 1 in match env with match 1 with | (hd::tl) -> | h::t -> ( if (t = []) then List.append l (simplify (SUM tl) env 0) match hd with else List.append (TIMES 1::[]) (simplify (SUM tl) env 0) | (x, c, p) -> | [] -> [] ( ) match elem with | [] -> deployEnv env 0 |(x2, c2, p2) -> ) if (flag = 0) then | TIMES lst -> if (x = x2 && p = p2) then (x, (c + c2), p)::tl ( else hd::(updateEnv elem tl flag) match 1st with else | (CONST c)::tl -> simplify (TIMES tl) (updateEnv ("const", c, 0) env 1) 1 if (x = x2) then (x, (c\*c2), (p + p2))::tl | (VAR x)::tl -> simplify (TIMES tl) (updateEnv (x, 1, 1) env 1) 1 else hd::(updateEnv elem tl flag) | (POWER (x, p))::tl -> simplify (TIMES tl) (updateEnv (x, 1, p) env 1) 1 ) | (SUM lst)::tl -> ) | [] -> elem::[] let 1 = simplify (SUM 1st) [] 0 in in match 1 with | h::t -> let rec doDiff : aexp \* string -> aexp if (t = []) then List.append l (simplify (TIMES tl) env 1) = fun (aexp, x) -> else List.append (SUM 1::[]) (simplify (TIMES tl) env 1) ((Sum lst)::tl) match aexp with - [] 1 [] | CONST \_ -> CONST 0 ) | VAR v -> | (TIMES lst)::tl -> simplify (TIMES (List.append lst tl)) env 1 if (x = v) then CONST 1 | [] -> deployEnv env 1 else CONST 0 ) | POWER (v, p) -> in if (p = 0) then CONST 0 else if (x = v) then TIMES ((CONST p)::POWER (v, p-1)::[]) let result = doDiff (aexp, x) in else CONST 0 match result with | TIMES lst -> | SUM \_ -> SUM (simplify result [] 0) ( | TIMES \_ -> TIMES (simplify result [] 1) match 1st with | \_ -> result



### The FixML System



**Correct Program** 

#### **Program Synthesis**

## Synthesizing Imperative Programs

• Specification is given as test cases

SAS'17

reverse(12) = 21, reverse(123) = 321



#### Performance

Better than humans for introductory programming tasks

Domain	No	Description	Vars		Inte	Eve	Time (sec)		
	110		IVars	AVars	ints	LAS	Base	Base+Opt	Ours
	1	Given <i>n</i> , return <i>n</i> !.	2	0	2	4	0.0	0.0	0.0
	2	Given $n$ , return $n!!$ (i.e., double factorial).	3	0	3	4	0.0	0.0	0.0
	3	Given <i>n</i> , return $\sum_{i=1}^{n} i$ .	3	0	2	4	0.1	0.0	0.0
	4	Given <i>n</i> , return $\sum_{i=1}^{n} i^2$ .	4	0	2	3	122.4	18.1	0.3
	5	Given <i>n</i> , return $\prod_{i=1}^{n} i^2$ .	4	0	2	3	102.9	13.6	0.2
	6	Given $a$ and $n$ , return $a^n$ .		0	2	4	0.7	0.1	0.1
	7	Given n and m, return $\sum_{i=n}^{m} i$ .	3	0	2	3	0.2	0.0	0.0
Tutorov	8	Given n and m, return $\prod_{i=n}^{m} i$ .	3	0	2	3	0.2	0.0	0.1
Integer	9	Count the number of digit for an integer.	3	0	3	3	0.0	0.0	0.0
	10	Sum the digits of an integer.	3	0	3	4	5.2	2.2	1.3
	11	Calculate product of digits of an intger.	3	0	3	3	0.7	2.3	0.3
	12	Count the number of binary digit of an integer.	2	0	3	3	0.0	0.0	0.0
	13	Find the <i>n</i> th Fibonacci number.	3	0	3	4	98.7	13.9	2.6
	14	Given n, return $\sum_{i=1}^{n} (\sum_{m=1}^{i} m)$ ).	3	0	2	4	$\perp$	324.9	37.6
	15	Given <i>n</i> , return $\prod_{i=1}^{n} (\prod_{m=1}^{i} m)$ ).	3	0	2	4	$\perp$	316.6	86.9
	16	Reverse a given integer.	3	0	3	3	$\perp$	367.3	2.5
	17	Find the sum of all elements of an array.	3	1	2	2	8.1	3.6	0.9
	18	Find the product of all elements of an array.	3	1	2	2	7.6	3.9	0.9
	19	Sum two arrays of same length into one array.	3	2	2	2	44.6	29.9	0.2
	20	Multiply two arrays of same length into one array.	3	2	2	2	47.4	26.4	0.3
	21	Cube each element of an array.	3	1	1	2	1283.3	716.1	13.0
A	22	Manipulate each element into 4th power.	3	1	1	2	1265.8	715.5	13.0
	23	Find a maximum element.	3	1	2	2	0.9	0.7	0.4
	24	Find a minimum element.	3	1	2	2	0.8	0.3	0.1
Allay	25	Add 1 to each element.	2	1	1	3	0.3	0.0	0.0
	26	Find the sum of square of each element.	3	1	2	2	2700.0	186.2	11.5
	27	Find the multiplication of square of each element.	3	1	1	2	1709.8	1040.3	12.6
	28	Sum the products of matching elements of two arrays.	3	2	1	3	20.5	38.7	1.5
	29	Sum the absolute values of each element.	2	1	1	2	45.0	50.5	12.1
	30	Count the number of each element.	3	1	3	2	238.9	1094.1	0.2
	Average							165.5	6.6





1JCAI'18



for i in N do: for j in N do: *if* (i = 1 || i = N || j = 1 || j = i || $j = N - i + 1 \mid j = N$ : print  $\bigstar$ else: print \_\_\_\_ print  $\leftarrow$ 



\*\*\*\*\*

```
for i in N do:

for j in 4 * N - i - 2 do:

if (j = 2 * N - i || j = 2 * N + i - 2 ||

j = 4 * N - i - 2 || j = i): print \bigstar

else: print \square

print \square
```

## Thank you!

- Research areas: programming languages, software engineering, software security
  - program analysis and testing
  - program synthesis and repair
- Publication: top-venues in PL, SE, Security, and AI:



 PLDI('12,'14), OOPSLA('15,'17,'17), TOPLAS('14,'16,'17), ICSE('17,'18), FSE'18, S&P'17, IJCAI('17,'18), etc

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