

# Final Exam (COSE 312 Compilers, Spring 2025)

Student Number:

Name:

Leave a blank when uncertain. Each correct answer gets you 1 point but you lose 1 point for each wrong answer.

- (1) Big-step operational semantics for **While** is compositional. **X**
- (2) The following function  $F$  has infinitely many fixed points. **O**

$$F(g) = \lambda s. \begin{cases} g(s) & \text{if } s(x) \neq 0 \\ s & \text{if } s(x) = 0 \end{cases}$$

- (3) Let  $w$  be the following loop:

while  $\neg(x = 0)$  do  $x := x - 1$

Then,

$$C[[w]](s) = \begin{cases} s[x \mapsto 0] & \text{if } s(x) \geq 0 \\ \text{undef} & \text{if } s(x) < 0 \end{cases}$$

**O**

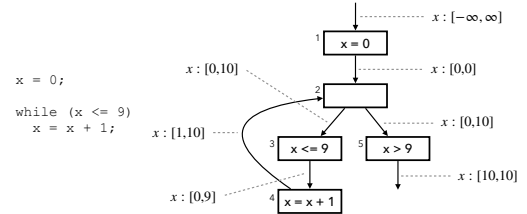
- (4)  $\emptyset$  is a chain. **O**
- (5) Every CPO has the least element, denoted  $\perp$ . **O**
- (6) Every CPO has the greatest element, denoted  $\top$ . **X**
- (7) The following function is continuous:

$$F_1(g) = \begin{cases} g_1 & \dots g = g_2 \\ g_2 & \dots \text{otherwise} \end{cases}$$

where  $g_1 \neq g_2$ . **X**

- (8) The semantic function  $C[[c]] : \text{State} \leftrightarrow \text{State}$  for commands is strict, i.e.,  $C[[c]](\perp) = \perp$ . **O**
- (9)  $C[[c]]$  is a partial function. **O**
- (10)  $\widehat{C}[[c]]$  is a partial function. **X**
- (11) Sound static analysis can prove the presence of bugs. **X**
- (12) The simple sign analysis discussed in class is guaranteed to terminate even for non-terminating programs. **O**
- (13) The simple sign domain,  $\{\top, \perp, \text{neg}, \text{zero}, \text{pos}\}$ , is a complete lattice. **O**
- (14) The interval domain is not a complete lattice. **X**
- (15) For some programs, interval analysis terminates without the use of widening. **O**
- (16) For some programs, concrete execution terminates but interval analysis without widening does not terminate. **O**
- (17) Widening and narrowing ensure termination with the least fixed point. **X**
- (18) Fixed point computation with narrowing follows a decreasing chain. **O**
- (19)  $[1, 2] =_{\widehat{=}} [1, 2]$ . **X**
- (20) The interval domain is a relational domain. **X**
- (21) For finite height domains with infinite elements, fixed point computation always terminates. **O**

- (22) The following analysis result represents the least fixed point; any result more precise than this would be unsound. **O**



- (23) Suppose programs  $P_1$  and  $P_2$  are semantically equivalent. Then, interval analysis is guaranteed to produce identical results for both programs. **X**
- (24) Consider the assignment  $lv := e$ , where assume the input abstract state is  $\hat{m}$  and  $\widehat{L}(lv)(\hat{m}) = \{x, y\}$ . Then, the abstract semantics that produces the following output state

$$\hat{m}[x \mapsto \widehat{E}(e)(\hat{m}), y \mapsto \widehat{E}(e)(\hat{m})]$$

is sound. **X**

- (25) It is sound to perform loop-invariant code motion when the reaching definition information is over-approximated. **O**
- (26) Reaching definition analysis is a forward, must analysis. **X**
- (27) Liveness analysis is a backward, may analysis. **O**
- (28) Exact def/use sets are not computable for Turing-complete languages. **O**
- (29) The available expressions analysis computes only the truly available expressions. **O**
- (30) In a must data-flow analysis, the join operator ( $\sqcup$ ) corresponds to the set union ( $\cup$ ). **X**
- (31) In a must data-flow analysis, the greatest fixed point corresponds to the most precise solution. **O**
- (32) A must data-flow analysis computes an increasing chain. **X**
- (33) Suppose the constant propagation analysis has computed the abstract state:
 
$$\{x \mapsto \top, y \mapsto 3, z \mapsto \top\}$$
 at a program point. This means that  $y$  is guaranteed to be constant 3 at that point no matter how the program is executed. **O**
- (34) The “busy” expression analysis mentioned in class is a must, backward analysis. **O**
- (35) Interval analysis is always at least as precise as constant propagation analysis. **O**
- (36) A may analysis (e.g., constant propagation) cannot be used to infer “must” program properties. **X**