

Homework 4

COSE212, Fall 2016

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Due: 11/18, 24:00

Problem 1 Write an interpreter for the following language:

Syntax

$$\begin{array}{l} P \rightarrow E \\ E \rightarrow n \\ \quad | \quad x \\ \quad | \quad E + E \\ \quad | \quad E - E \\ \quad | \quad E * E \\ \quad | \quad E / E \\ \quad | \quad \text{iszero } E \\ \quad | \quad \text{read} \\ \quad | \quad \text{if } E \text{ then } E \text{ else } E \\ \quad | \quad \text{let } x = E \text{ in } E \\ \quad | \quad \text{letrec } f(x) = E \text{ in } E \\ \quad | \quad \text{proc } x E \\ \quad | \quad E E \\ \quad | \quad E \langle x \rangle \\ \quad | \quad \text{set } x = E \\ \quad | \quad E; E \\ \quad | \quad \text{begin } E \text{ end} \end{array}$$

Semantics

$$\begin{array}{l} Val = \mathbb{Z} + Bool + Procedure + RecProcedure \\ Procedure = Var \times E \times Env \\ RecProcedure = Var \times Var \times E \times Env \\ \rho \in Env = Var \rightarrow Loc \\ \sigma \in Mem = Loc \rightarrow Val \end{array}$$

$$\begin{array}{c}
\frac{}{\rho, \sigma \vdash n \Rightarrow n, \sigma} \\
\frac{}{\rho, \sigma \vdash x \Rightarrow \sigma(\rho(x)), \sigma} \\
\frac{\rho, \sigma_0 \vdash E_1 \Rightarrow n_1, \sigma_1 \quad \rho, \sigma_1 \vdash E_2 \Rightarrow n_2, \sigma_2}{\rho, \sigma_0 \vdash E_1 + E_2 \Rightarrow n_1 + n_2, \sigma_2} \\
\frac{\rho, \sigma_0 \vdash E_1 \Rightarrow n_1, \sigma_1 \quad \rho, \sigma_1 \vdash E_2 \Rightarrow n_2, \sigma_2}{\rho, \sigma_0 \vdash E_1 - E_2 \Rightarrow n_1 - n_2, \sigma_2} \\
\frac{\rho, \sigma_0 \vdash E_1 \Rightarrow n_1, \sigma_1 \quad \rho, \sigma_1 \vdash E_2 \Rightarrow n_2, \sigma_2}{\rho, \sigma_0 \vdash E_1 * E_2 \Rightarrow n_1 * n_2, \sigma_2} \\
\frac{\rho, \sigma_0 \vdash E_1 \Rightarrow n_1, \sigma_1 \quad \rho, \sigma_1 \vdash E_2 \Rightarrow n_2, \sigma_2}{\rho, \sigma_0 \vdash E_1 / E_2 \Rightarrow n_1 / n_2, \sigma_2} \\
\frac{\rho, \sigma_0 \vdash E \Rightarrow 0, \sigma_1}{\rho, \sigma_0 \vdash \text{iszero } E \Rightarrow \text{true}, \sigma_1} \\
\frac{\rho, \sigma_0 \vdash E \Rightarrow n, \sigma_1}{\rho, \sigma_0 \vdash \text{iszero } E \Rightarrow \text{false}, \sigma_1} \quad n \neq 0 \\
\frac{\rho, \sigma_0 \vdash E_1 \Rightarrow \text{true}, \sigma_1 \quad \rho, \sigma_1 \vdash E_2 \Rightarrow v, \sigma_2}{\rho, \sigma_0 \vdash \text{if } E_1 \text{ then } E_2 \text{ else } E_3 \Rightarrow v, \sigma_2} \\
\frac{\rho, \sigma_0 \vdash E_1 \Rightarrow \text{false}, \sigma_1 \quad \rho, \sigma_1 \vdash E_3 \Rightarrow v, \sigma_2}{\rho, \sigma_0 \vdash \text{if } E_1 \text{ then } E_2 \text{ else } E_3 \Rightarrow v, \sigma_2} \\
\frac{\rho, \sigma_0 \vdash E_1 \Rightarrow v_1, \sigma_1 \quad [x \mapsto l]\rho, [l \mapsto v_1]\sigma_1 \vdash E_2 \Rightarrow v, \sigma_2 \quad l \notin \text{Dom}(\sigma_1)}{\rho, \sigma_0 \vdash \text{let } x = E_1 \text{ in } E_2 \Rightarrow v, \sigma_2} \\
\frac{\boxed{\text{Complete the definition.}}}{\rho, \sigma_0 \vdash \text{letrec } f(x) = E_1 \text{ in } E_2 \Rightarrow} \\
\frac{}{\rho, \sigma \vdash \text{proc } x E \Rightarrow (x, E, \rho), \sigma} \\
\frac{\rho, \sigma_0 \vdash E_1 \Rightarrow (x, E, \rho'), \sigma_1 \quad \rho, \sigma_1 \vdash E_2 \Rightarrow v, \sigma_2 \quad [x \mapsto l]\rho', [l \mapsto v]\sigma_2 \vdash E \Rightarrow v', \sigma_3 \quad l \notin \text{Dom}(\sigma_2)}{\rho, \sigma_0 \vdash E_1 E_2 \Rightarrow v', \sigma_3} \\
\frac{\rho, \sigma_0 \vdash E_1 \Rightarrow (f, x, E, \rho'), \sigma_1 \quad \boxed{\text{Complete the definition.}}}{\rho, \sigma_0 \vdash E_1 E_2 \Rightarrow} \\
\frac{\rho, \sigma_0 \vdash E_1 \vdash (x, E, \rho'), \sigma_1 \quad [x \mapsto \rho(y)]\rho', \sigma_1 \vdash E \Rightarrow v', \sigma_2}{\rho, \sigma_0 \vdash E_1 \langle y \rangle \Rightarrow v', \sigma_2}
\end{array}$$

$$\begin{array}{c}
\rho, \sigma_0 \vdash E_1 \vdash (f, x, E, \rho'), \sigma_1 \quad \boxed{\text{Complete the definition.}} \\
\hline
\rho, \sigma_0 \vdash E_1 \langle y \rangle \Rightarrow \\
\frac{\rho, \sigma_0 \vdash E \Rightarrow v, \sigma_1}{\rho, \sigma_0 \vdash \mathbf{set} \ x = E \Rightarrow v, [\rho(x) \mapsto v] \sigma_1} \\
\frac{\rho, \sigma_0 \vdash E_1 \Rightarrow v_1, \sigma_1 \quad \rho, \sigma_1 \vdash E_2 \Rightarrow v_2, \sigma_2}{\rho, \sigma_0 \vdash E_1; E_2 \Rightarrow v_2, \sigma_2} \\
\frac{\rho, \sigma_0 \vdash E \Rightarrow v, \sigma_1}{\rho, \sigma_0 \vdash \mathbf{begin} \ E \ \mathbf{end} \Rightarrow v, \sigma_1}
\end{array}$$

Complete the holes in the semantic definitions and implement an interpreter for the defined language.