AAA616: Program Analysis

Lecture 8 — Pointer Analysis

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Topics

- Pointer analysis
- Constraint-based analysis
- Interprocedural analysis
- Analysis of higher-order programs
- Context-sensitivity

Motivating Example

Reasoning about any real programs needs pointer reasoning: e.g.,

```
y = 2;
*p = 3;
*q = 4;
```

x = 1:

What is the value of x + y after the last statement?

- p = &x and q = &y:
- p = &x and $q \neq \&y$:
- $p \neq \&x$ and q = &y:
- $ullet p
 eq \& x ext{ and } q
 eq \& y$:

Pointer Analysis

- Static program analysis that computes the set of memory locations (objects) that a pointer variable may point to at runtime.
- One of the most important static analyses: all interesting questions on program reasoning eventually need pointer analysis.
 - ► E.g., control-flows, data-flows, types, information-flows, etc

Allocation-Site Abstraction

Memory locations are unbounded. Consider the program:

- In program execution, new objects are allocated repeatedly.
- In pointer analysis, objects get abstracted to their allocation sites.
- Thus, a pointer analysis would produce the result:

$$x \mapsto \{l_1\}, y \mapsto \{l_1\}, a \mapsto \{l_2\}, b \mapsto \{l_2\}, p \mapsto \{l_1, l_2\}$$

Pointer Analysis in Datalog

 Pointer analysis is expressed as subset constraints. The analysis is to compute the smallest solution of the constraints. E.g.,

```
a = new A();
b = a;
```

- We use the Datalog language to express such constraints.
- Datalog is a declarative logic programming language, which has application in many fields, e.g., database, information extraction, networking, program analysis, security, etc.

Syntax of Datalog

A Datalog program is a sequence of constraints:

$$P ::= \bar{c}$$

 A constraint consists of a head of a literal and a body of a list of literals:

$$c ::= l := \bar{l}$$

A constraint represents a horn clause (a disjunction of literals with at most one positive, unnegated, literal):

$$l \vee \neg l_1 \vee \neg l_2 \vee \cdots \vee \neg l_n \iff l \leftarrow l_1 \wedge l_2 \wedge \cdots \wedge l_n$$

A literal is a relation with arguments:

$$l ::= r(\bar{a})$$

where an argument is either a variable or constant.

Example

```
parent(bill, mary).
parent(mary, john).
ancestor(X,Y) :- parent(X,Y).
ancestor(X,Y) :- parent(X,Z), ancestor(Z,Y).
```

Semantics of Datalog

A Datalog program denotes a set of ground literals:

$$\llbracket P
rbracket \in \wp(G)$$

where G is the set of ground literals (literals without variables).

• A Datalog rule $l:=l_1,\ldots,l_n$ denotes the function:

$$f_{l:-l_1,...,l_n}(X) = \{\sigma(l_0) \mid \sigma(l_k) \in X \text{ for } 1 \leq k \leq n\}$$

where σ is a variable substitution.

ullet The semantics of P is defined as the least fixed point of F_P :

$$\llbracket P
rbracket = \mathit{lfp}\,F_P \;\; ext{where} \; F_P(X) = X \cup igcup_{c \in P} f_c(X)$$

• The semantics is monotone:

$$P_1 \subseteq P_2 \implies \llbracket P_1 \rrbracket \subseteq \llbracket P_2 \rrbracket$$

Programs as Relations

Without procedures, a program can be represented by a set of the relations:

```
ALLOC (var: V, heap: H)
 Move (to: V, from: V)
 Load(to: V, base: V, fld: F)
 Store(base: V, fld: F, from: V)
domains:

    V is a set of program variables

  • H is a set of heap abstractions (i.e. allocation sites)

    F is a set of fields

a = new A();
b = new B();
c = a:
a.f = b:
d = c.f:
```

Simple Pointer Analysis

Pointer analysis computes the set of points-to relations:

```
egin{aligned} 	ext{VARPOINTSTO} & (var: V, heap: H) \ 	ext{FLDPOINTSTO} & (base H: H, fld: F, heap: H) \end{aligned}
```

Analysis rules:

```
VarPointsTo(var, heap) \leftarrow Alloc(var, heap)

VarPointsTo(to, heap) \leftarrow Move(to, from), VarPointsTo(from, heap)

FldPointsTo(baseH, fld, heap) \leftarrow Store(base, fld, from), VarPointsTo(from, heap), VarPointsTo(from, heap), VarPointsTo(from, heap).
```

Exercise) Define the rule for LOAD.

Interprocedural Analysis

Domains:

- ullet V is a set of program variables
- H is a set of heap abstractions (i.e. allocation sites)
- F is a set of fields
- M is a set of method identifiers
- ullet S is a set of method signatures (including name, type signature)
- I is a set of instructions
- T is a set of class types
- ullet N is the set of natural numbers

Interprocedural Analysis (First-Order)

• Input relations:

```
ALLOC (var: V, heap: H, inMeth: M)
  Move (to: V, from: V)
  Load(to: V, base: V, fld: F)
  Store(base: V, fld: F, from: V)
  CallGraph(invo:I, meth:M)
  Reachable(meth: M)
  FORMALARG(meth: M, i: \mathbb{N}, arg: V)
  ActualArg(invo:I,i:\mathbb{N},arg:V)
  FORMALRETURN(meth: M, ret: V)
  ACTUALRETURN(invo:I,var:V)
Output relations:
  VARPOINTSTO (var: V, heap: H)
  FLDPOINTSTO (baseH:H,fld:F,heap:H)
  InterProcAssign (to: V, from: V)
```

Analysis Rules

```
VARPOINTSTo(var, heap) \leftarrow
  Reachable (meth), Alloc (var, heap, meth)
VARPOINTSTo(to, heap) \leftarrow
  Move(to, from), VarPointsTo(from, heap)
FLDPOINTSTO(baseH, fld, heap) \leftarrow
  Store(base, fld, from), VarPointsTo(from, heap),
  VarPointsTo(base, baseH).
VARPOINTSTo(to, heap) \leftarrow
  Load(to, base, fld), VarPointsTo(base, baseH),
  FLDPOINTSTO(baseH, fld, heap).
INTERPROCASSIGN(to, from) \leftarrow CallGraph(invo, meth),
  FORMALARG(meth, n, to), ACTUALARG(invo, n, from).
INTERPROCASSIGN(to, from) \leftarrow CallGraph(invo, meth),
  FORMALRETURN (meth, from), ACTUALRETURN (invo, to).
VARPOINTSTo(to, heap) \leftarrow
  INTERPROCASSIGN(to, from), VARPOINTSTO(from, heap).
```

Example

```
Object f(Object p) {
  return p;
}
a = new A();
b = f(a);
```

Interprocedural Analysis (Higher-Order)

Input relations:

```
ALLOC (var: V, heap: H, inMeth: M)
   Move (to: V, from: V)
   Load(to: V, base: V, fld: F)
   Store(base: V, fld: F, from: V)
   VCALL(base: V, sig: S, invo: I, inMeth: M)
   FORMALARG(meth: M, i: \mathbb{N}, arg: V)
   ACTUALARG(invo:I,i:\mathbb{N},arg:V)
   FORMALRETURN(meth: M, ret: V)
   ACTUALRETURN (invo: I, var: V)
   This Var (meth: M, this: V)
   \text{HEAPTYPE}(heap: H, type: T)
   LOOKUP(type: T, sig: S, meth: M)
Output relations:
   VARPOINTSTO (var: V, heap: H)
   FLDPOINTSTO (baseH:H,fld:F,heap:H)
   InterProcAssign (to: V, from: V)
   Callgraph (invo: I, meth: M)
   Reachable (meth: M)
```

Analysis Rules

A new rule for VCALL whose main job is to update call-graph:

```
REACHABLE(toMeth),
VARPOINTSTO(this, heap),
CALLGRAPH(invo, toMeth) \leftarrow
VCALL(base, sig, invo, inMeth), REACHABLE(inMeth),
VARPOINTSTO(base, heap),
HEAPTYPE(heap, heapT), LOOKUP(heapT, sig, toMeth),
THISVAR(toMeth, this).
```

The analysis performs on-the-fly call-graph construction.

- Pointer analysis and call-graph construction are closed inter-connected in object-oriented and higher-order languages. For example, to resolve call obj.fun(), we need pointer analysis. To compute points-to set of a in f(Object a){...}, we need call-graph.
- This global fixed point computation increases precision of both.

Example

```
class C {
  Object id(Object v) { return v; }
}
class B {
 void m (){
    C c = new C();
    D d = c.id(new D());
    E = c.id(new E());
public class A {
 void f(){
    B b = new B();
    b.m();
    b.m();
```

Need for Context-Sensitivity

Our current analysis is context-insensitive:

```
class C { Object id(Object v){ return v; } }
class B {
  void m () {
        C c = new C();
        D d = c.id(new D());
        E e = c.id(new E()); }}
public class A {
  void f() {
        B b = new B();
        b.m();
        b.m(); }}
```

- To achieve more precision, we can quality the analysis results with context information. Two kinds of contexts:
 - ► Calling context for qualifying local variables
 - Heap context for qualifying heap abstractions

Domains for Context-Sensitive Analysis

- ullet V is a set of program variables
- *H* is a set of heap abstractions (i.e. allocation sites)
- ullet M is a set of method identifiers
- ullet S is a set of method signatures (including name, type signature)
- F is a set of fields
- I is a set of instructions
- T is a set of class types
- N is the set of natural numbers
- C is a set of calling contexts
- HC is a set of heap contexts

Output Relations for Context-Sensitive Analysis

The output relations are modified to add contexts:

```
VARPOINTSTO(var: V, ctx: C, heap: H, hctx: HC)
CALLGRAPH(invo: I, callerCtx: C, meth: M, calleeCtx: C)
FLDPOINTSTO(baseH: H, baseHCtx: HC, fld: F, heap: H, hctx: HC)
INTERPROCASSIGN(to: V, toCtx: C, from: V, fromCtx: C)
REACHABLE(meth: M, ctx: C)
```

Context constructors:

```
Record (heap: H, ctx: C) = newHCtx: HC

Merge (heap: H, hctx: HC, invo: I, ctx: C) = newCtx: C
```

- Record generates heap contexts.
- Merge generates calling contexts.
- Different choices of them yield different context-sensitivity flavors.

Analysis Rules

```
Record (heap, ctx) = hctx,
VarPointsTo(var, ctx, heap, hctx) \leftarrow
 REACHABLE (meth, ctx), ALLOC (var, heap, meth).
VarPointsTo(to, ctx, heap, hctx) \leftarrow
 MOVE(to, from), VARPOINTSTO(from, ctx, heap, hctx).
FLDPOINTSTO(baseH, baseHCtx, fld, heap, hctx) \leftarrow
 STORE(base, fld, from), VARPOINTSTO(from, ctx, heap, hctx),
 VARPOINTSTO(base, ctx, baseH, baseHCtx).
VarPointsTo(to, ctx, heap, hctx) \leftarrow
 LOAD(to, base, fld), VARPOINTSTO(base, ctx, baseH, baseHCtx),
 FLDPOINTSTO(baseH, baseHCtx, fld, heap, hctx).
```

Analysis Rules

```
Merge (heap, hctx, invo, callerCtx) = calleeCtx,
Reachable(toMeth, calleeCtx),
VarPointsTo(this, calleeCtx, heap, hctx),
CallGraph(invo, callerCtx, toMeth, calleeCtx) \leftarrow
 VCall(base, sig, invo, inMeth), Reachable(inMeth, callerCtx),
 VARPOINTSTO(base, callerCtx, heap, hctx),
 \text{HEAPTYPE}(heap, heapT), \text{LOOKUP}(heapT, siq, toMeth),
 ThisVar(toMeth. this).
INTERPROCASSIGN(to, calleeCtx, from, callerCtx) \leftarrow
 Callgraph (invo, caller Ctx, meth, callee Ctx),
 FORMALARG(meth, n, to), ACTUALARG(invo, n, from).
InterProcAssign(to, callerCtx, from, calleeCtx) \leftarrow
 Callgraph (invo, caller Ctx, meth, callee Ctx),
 FORMALRETURN (meth, from), ACTUALRETURN (invo, to).
VarPointsTo(to, toCtx, heap, hctx) \leftarrow
 INTERPROCASSIGN(to, toCtx, from, fromCtx),
 VARPOINTSTO(from, fromCtx, heap, hctx).
```

Call-Site-Sensitivity (aka., k-CFA)

- The best-known flavor of context-sensitivity. It uses call-sites as contexts.
- In k-CFA, a method gets analyzed with the context that is a sequence
 of the last k call-sites (the current call-site of the method, the
 call-site of the caller method, the call-site of the caller method's
 caller, etc, up to a pre-defined depth, k).

Call-Site-Sensitivity

• 1-call-site sensitive with context-insensitive heap:

$$\begin{split} C &= I, \qquad HC = \{\star\} \\ \mathsf{Record}(heap, ctx) &= \star \\ \mathsf{Merge}(heap, hctx, invo, ctx) &= invo \end{split}$$

• 1-call-site sensitive with context-sensitive heap:

$$C = I, \qquad HC = I$$

$$\mathsf{Record}(heap, ctx) = ctx$$

$$\mathsf{Merge}(heap, hctx, invo, ctx) = invo$$

• 2-call-site sensitive with 1-call-site-sensitive heap:

$$C = I \times I, \qquad HC = I$$

 $\mathsf{Record}(heap, ctx) = first(ctx)$
 $\mathsf{Merge}(heap, hctx, invo, ctx) = pair(invo, first(ctx))$

Example

```
class C { Object id(Object v){ return v; } }
class B {
 void m (){
   C c = new C();
   D d = c.id(new D());
   E = c.id(new E());
public class A {
 void f(){
   B b = new B();
   b.m();
   b.m();
```

Object-Sensitivity

- The dominant flavor of context-sensitivity for object-oriented languages.
- It uses object abstractions (i.e. allocation sites) as contexts, qualifying a method's local variables with the allocation site of the receiver object of the method call.

```
class A { void m() { return; } }
...
b = new B();
b.m();
```

The context of m is the allocation site of b.

Exercise

```
class S {
  Object id(Object a) { return a; }
  Object id2(Object a) { return id(); }
}
class C extends S {
  void fun1() {
    Object a1 = new A1();
    Object b1 = id2(a1);
  }}
class D extends S {
  void fun2() {
    Object a2 = new A2();
    Object b2 = id2(a2);
  }}
```

- What is the result of 1-call-site-sensitive analysis?
- What is the result of 1-object-sensitive analysis?
- Explain the strength of object-sensitivity over call-site-sensitivity.

Object-Sensitivity

1-object-sensitive with context-insensitive heap:

$$\begin{split} C &= H, & HC &= \{\star\} \\ \mathsf{Record}(heap, ctx) &= \star \\ \mathsf{Merge}(heap, hctx, invo, ctx) &= heap \end{split}$$

2-object-sensitive with 1-context-sensitive heap:

$$\begin{split} C &= H \times H, \qquad HC = H \\ \mathsf{Record}(heap, ctx) &= first(ctx) \\ \mathsf{Merge}(heap, hctx, invo, ctx) &= pair(heap, hctx) \end{split}$$

Example

```
class D{} class E{}
class C { Object id(Object v) { return v; } }
class B {
  Object id(Object v) {
   C c = new C(); // 13, heap objects: ([11],13), ([12],13)
    return c.id(v); // calling contexts: [13,11], [13,12]
class A {
  void m () {
   B b1 = new B(); // 11
    B b2 = new B(); // 12
   D d = b1.id (new D()); // calling contexts: 11
   E = b2.id (new E()); // calling contexts: 12
```

Summary

We have covered a number of key concepts in program analysis:

- Pointer analysis
- Constraint-based analysis
- Interprocedural analysis
- Analysis of higher-order programs
- Context-sensitivity

For more details, see

Yannis Smaragdakis and George Balatsouras. Pointer Analysis.
 Foundations and Trends in Programming Languages. 2(1). 2015.