

# COSE212: Programming Languages

## Lecture 8 — Design and Implementation of PLs (4) States

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## Motivating Example

- How can we compute the number of times `f` has been called?

```
let f = proc (x) (x)
in (f (f 1))
```

- Does the following program work?

```
let counter = 0
in let f = proc (x) (let counter = counter + 1
                    in x)
   in let a = (f (f 1))
      in counter
```

- The language should support *effects*.
- Effects are implemented by introducing *memory (store)* and *locations (reference)*.

# Computational Effects

Programming languages support effects explicitly or implicitly.

- Explicit languages provide a clear account of allocation, dereference, and mutation of memory cells, e.g., ML.
- In implicit languages, they are built-in, e.g., C and Java.

# A Language with Explicit References

$$\begin{aligned} P &\rightarrow E \\ E &\rightarrow n \mid x \\ &\mid E + E \mid E - E \\ &\mid \text{zero? } E \mid \text{if } E \text{ then } E \text{ else } E \\ &\mid \text{let } x = E \text{ in } E \\ &\mid \text{proc } x E \mid E E \\ &\mid \text{ref } E \\ &\mid ! E \\ &\mid E := E \\ &\mid E; E \end{aligned}$$

- $\text{ref } E$  allocates a new location and store the value of  $E$  in it.
- $! E$  returns the contents of the location that  $E$  refers to.
- $E_1 := E_2$  changes the contents of the location ( $E_1$ ) by the value of  $E_2$ .

## Example 1

- `let counter = ref 0`  
  `in let f = proc (x) (counter := !counter + 1; !counter)`  
    `in let a = (f 0)`  
      `in let b = (f 0)`  
        `in (a - b)`
- `let f = let counter = ref 0`  
      `in proc (x) (counter := !counter + 1; !counter)`  
`in let a = (f 0)`  
   `in let b = (f 0)`  
      `in (a - b)`
- `let f = proc (x) (let counter = ref 0`  
                  `in (counter := !counter + 1; !counter))`  
`in let a = (f 0)`  
   `in let b = (f 0)`  
      `in (a - b)`

## Example 2

We can make chains of references:

```
let x = ref (ref 0)
in (!x := 11; !(!x))
```

# Semantics

Memory is modeled as a finite map from locations to values:

$$\begin{aligned} \mathit{Val} &= \mathbb{Z} + \mathit{Bool} + \mathit{Procedure} + \mathit{Loc} \\ \mathit{Procedure} &= \mathit{Var} \times \mathit{E} \times \mathit{Env} \\ \rho \in \mathit{Env} &= \mathit{Var} \rightarrow \mathit{Val} \\ \sigma \in \mathit{Mem} &= \mathit{Loc} \rightarrow \mathit{Val} \end{aligned}$$

Semantics rules describe memory effects:

$$\rho, \sigma \vdash E \Rightarrow v, \sigma'$$

# Semantics

Existing rules are enriched with stores:

$$\frac{}{\rho, \sigma \vdash n \Rightarrow n, \sigma} \quad \frac{}{\rho, \sigma \vdash x \Rightarrow \rho(x), \sigma}$$

$$\frac{\rho, \sigma_0 \vdash E_1 \Rightarrow n_1, \sigma_1 \quad \rho, \sigma_1 \vdash E_2 \Rightarrow n_2, \sigma_2}{\rho, \sigma_0 \vdash E_1 + E_2 \Rightarrow n_1 + n_2, \sigma_2}$$

$$\frac{\rho, \sigma_0 \vdash E \Rightarrow 0, \sigma_1}{\rho, \sigma_0 \vdash \text{zero? } E \Rightarrow \text{true}, \sigma_1} \quad \frac{\rho, \sigma_0 \vdash E \Rightarrow n, \sigma_1}{\rho, \sigma_0 \vdash \text{zero? } E \Rightarrow \text{false}, \sigma_1} \quad n \neq 0$$

$$\frac{\rho, \sigma_0 \vdash E_1 \Rightarrow \text{true}, \sigma_1 \quad \rho, \sigma_1 \vdash E_2 \Rightarrow v, \sigma_2}{\rho, \sigma_0 \vdash \text{if } E_1 \text{ then } E_2 \text{ else } E_3 \Rightarrow v, \sigma_2}$$

$$\frac{\rho, \sigma_0 \vdash E_1 \Rightarrow v_1, \sigma_1 \quad [x \mapsto v_1]\rho, \sigma_1 \vdash E_2 \Rightarrow v, \sigma_2}{\rho, \sigma_0 \vdash \text{let } x = E_1 \text{ in } E_2 \Rightarrow v, \sigma_2}$$

$$\frac{}{\rho, \sigma \vdash \text{proc } x \ E \Rightarrow (x, E, \rho), \sigma}$$

$$\frac{\rho, \sigma_0 \vdash E_1 \vdash (x, E, \rho'), \sigma_1 \quad \rho, \sigma_1 \vdash E_2 \Rightarrow v, \sigma_2 \quad [x \mapsto v]\rho', \sigma_2 \vdash E \Rightarrow v', \sigma_3}{\rho, \sigma_0 \vdash E_1 \ E_2 \Rightarrow v', \sigma_3}$$



# Semantics

Rules for new constructs:

$$\frac{\rho, \sigma_0 \vdash E \Rightarrow v, \sigma_1}{\rho, \sigma_0 \vdash \text{ref } E \Rightarrow l, [l \mapsto v]\sigma_1} \quad l \notin \text{Dom}(\sigma_1)$$

$$\frac{\rho, \sigma_0 \vdash E \Rightarrow l, \sigma_1}{\rho, \sigma_0 \vdash ! E \Rightarrow \sigma_1(l), \sigma_1}$$

$$\frac{\rho, \sigma_0 \vdash E_1 \Rightarrow l, \sigma_1 \quad \rho, \sigma_1 \vdash E_2 \Rightarrow v, \sigma_2}{\rho, \sigma_0 \vdash E_1 := E_2 \Rightarrow v, [l \mapsto v]\sigma_2}$$

$$\frac{\rho, \sigma_0 \vdash E_1 \Rightarrow v_1, \sigma_1 \quad \rho, \sigma_1 \vdash E_2 \Rightarrow v_2, \sigma_2}{\rho, \sigma_0 \vdash E_1; E_2 \Rightarrow v_2, \sigma_2}$$

## Example

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$$\rho, \sigma_0 \vdash \text{let } x = \text{ref } (\text{ref } 0) \text{ in } (!x := 11; !(!x)) \Rightarrow$$

# A Language with Implicit References

$$\begin{array}{l} P \rightarrow E \\ E \rightarrow n \mid x \\ \quad | E + E \mid E - E \\ \quad | \text{zero? } E \mid \text{if } E \text{ then } E \text{ else } E \\ \quad | \text{let } x = E \text{ in } E \\ \quad | \text{proc } x E \mid E E \\ \quad | \text{set } x = E \\ \quad | E; E \end{array}$$

- Every variable is mutable (i.e., changeable).
- $\text{set } x = E$  change the contents of  $x$  by the value of  $E$ .
- Locations are created with each binding operation: call and let.

## Examples

- ```
let f = let count = 0
        in proc (x) (set count = count + 1; count)
in let a = (f 0)
    in let b = (f 0)
        in a - b
```
- ```
let f = proc (x)
        proc (y)
          (set x = x + 1; x - y)
in ((f 44) 33)
```

# Semantics

Every variable denotes a reference:

$$\begin{aligned} \mathit{Val} &= \mathbb{Z} + \mathit{Bool} + \mathit{Procedure} \\ \mathit{Procedure} &= \mathit{Var} \times \mathit{E} \times \mathit{Env} \\ \rho \in \mathit{Env} &= \mathit{Var} \rightarrow \mathit{Loc} \\ \sigma \in \mathit{Mem} &= \mathit{Loc} \rightarrow \mathit{Val} \end{aligned}$$

# Semantics

$$\frac{}{\rho, \sigma \vdash n \Rightarrow n, \sigma} \quad \frac{}{\rho, \sigma \vdash x \Rightarrow \sigma(\rho(x)), \sigma}$$

$$\frac{\rho, \sigma_0 \vdash E_1 \Rightarrow n_1, \sigma_1 \quad \rho, \sigma_1 \vdash E_2 \Rightarrow n_2, \sigma_2}{\rho, \sigma_0 \vdash E_1 + E_2 \Rightarrow n_1 + n_2, \sigma_2}$$

$$\frac{\rho, \sigma_0 \vdash E \Rightarrow 0, \sigma_1}{\rho, \sigma_0 \vdash \text{zero? } E \Rightarrow \text{true}, \sigma_1} \quad \frac{\rho, \sigma_0 \vdash E_1 \Rightarrow \text{true}, \sigma_1 \quad \rho, \sigma_1 \vdash E_2 \Rightarrow v, \sigma_2}{\rho, \sigma_0 \vdash \text{if } E_1 \text{ then } E_2 \text{ else } E_3 \Rightarrow v, \sigma_2}$$

$$\frac{}{\rho, \sigma \vdash \text{proc } x \ E \Rightarrow (x, E, \rho), \sigma} \quad \frac{\rho, \sigma_0 \vdash E \Rightarrow v, \sigma_1}{\rho, \sigma_0 \vdash \text{set } x = E \Rightarrow v, [\rho(x) \mapsto v]\sigma_1}$$

$$\frac{\rho, \sigma_0 \vdash E_1 \Rightarrow v_1, \sigma_1 \quad [x \mapsto l]\rho, [l \mapsto v_1]\sigma_1 \vdash E_2 \Rightarrow v, \sigma_2}{\rho, \sigma_0 \vdash \text{let } x = E_1 \text{ in } E_2 \Rightarrow v, \sigma_2} \quad l \notin \text{Dom}(\sigma_1)$$

$$\frac{\rho, \sigma_0 \vdash E_1 \vdash (x, E, \rho'), \sigma_1 \quad \rho, \sigma_1 \vdash E_2 \Rightarrow v, \sigma_2 \quad [x \mapsto l]\rho', [l \mapsto v]\sigma_2 \vdash E \Rightarrow v', \sigma_3}{\rho, \sigma_0 \vdash E_1 \ E_2 \Rightarrow v', \sigma_3} \quad l \notin \text{Dom}(\sigma_2)$$

$$\frac{\rho, \sigma_0 \vdash E_1 \Rightarrow v_1, \sigma_1 \quad \rho, \sigma_1 \vdash E_2 \Rightarrow v_2, \sigma_2}{\rho, \sigma_0 \vdash E_1; E_2 \Rightarrow v_2, \sigma_2}$$

## Example

```
let f = let count = 0
        in proc (x) (set count = count + 1; count)
in let a = (f 0)
    in let b = (f 0)
        in a - b
```

## Call-By-Value Parameter-Passing

What is the value of the following program?

```
let p = proc (x) (set x = 4)
in let a = 3
    in ((p a); a)
```

The call semantics:

$$\frac{\rho, \sigma_0 \vdash E_1 \vdash (x, E, \rho'), \sigma_1 \quad \rho, \sigma_1 \vdash E_2 \Rightarrow v, \sigma_2 \quad [x \mapsto l]\rho', [l \mapsto v]\sigma_2 \vdash E \Rightarrow v', \sigma_3}{\rho, \sigma_0 \vdash E_1 E_2 \Rightarrow v', \sigma_3} \quad l \notin \text{Dom}(\sigma_2)$$

Call-by-value parameter-passing:

- The formal parameter refers to a new location containing the value of the actual parameter.
- The most commonly used form of parameter-passing.



## Call-By-Reference Parameter-Passing

The location of the caller's variable is passed, rather than the contents of the variable.

- Extend the syntax:

$$\begin{array}{l} E \rightarrow \vdots \\ | \quad E \ E \\ | \quad E \langle y \rangle \end{array}$$

- Extend the semantics:

$$\frac{\rho, \sigma_0 \vdash E_1 \vdash (x, E, \rho'), \sigma_1 \quad [x \mapsto \rho(y)]\rho', \sigma_1 \vdash E \Rightarrow v', \sigma_2}{\rho, \sigma_0 \vdash E_1 \langle y \rangle \Rightarrow v', \sigma_2}$$

## Examples

- ```
let p = proc (x) (set x = 4)
  in let a = 3
      in ((p <a>); a)
```
- ```
let f = proc (x) (set x = 44)
  in let g = proc (y) (f <y>)
      in let z = 55
          in ((g <z>); z)
```
- ```
let swap = proc (x) proc (y)
              let temp = x
                in (set x = y; set y = temp)
  in let a = 33
      in let b = 44
          in (((swap <a>) <b>); (a-b))
```

## Variable Aliasing

More than one call-by-reference parameter may refer to the same location:

```
let b = 3
in let p = proc (x) proc (y)
      (set x = 4; y)
  in ((p <b>) <b>)
```

- A *variable aliasing* is created:  $x$  and  $y$  refer to the same location
- With aliasing, reasoning about program behavior is very difficult, because an assignment to one variable may change the value of another.

## cf) Eager vs. Lazy Evaluation

```
letrec infinite-loop (x) = infinite-loop (x)
in let f = proc (x) (1)
    in (f (infinite-loop 0))
```

- In eager evaluation, procedure arguments are completely evaluated before passing them to the procedure.
- In lazy evaluation, evaluation of arguments is delayed until it is needed by the procedure body.
- Shortcoming of lazy evaluation?

# Summary

Our current language supports

- expressions, statements,
- procedures, recursion,
- parameter-passing variations: call-by-value, call-by-reference.